



UNIVERSITY OF  
CAMBRIDGE

Surface Microstructure and Fracture Group:  
*Fracture & Shock*

From static to dynamic  
(and in-between)

*- the response of polymer bonded explosives*

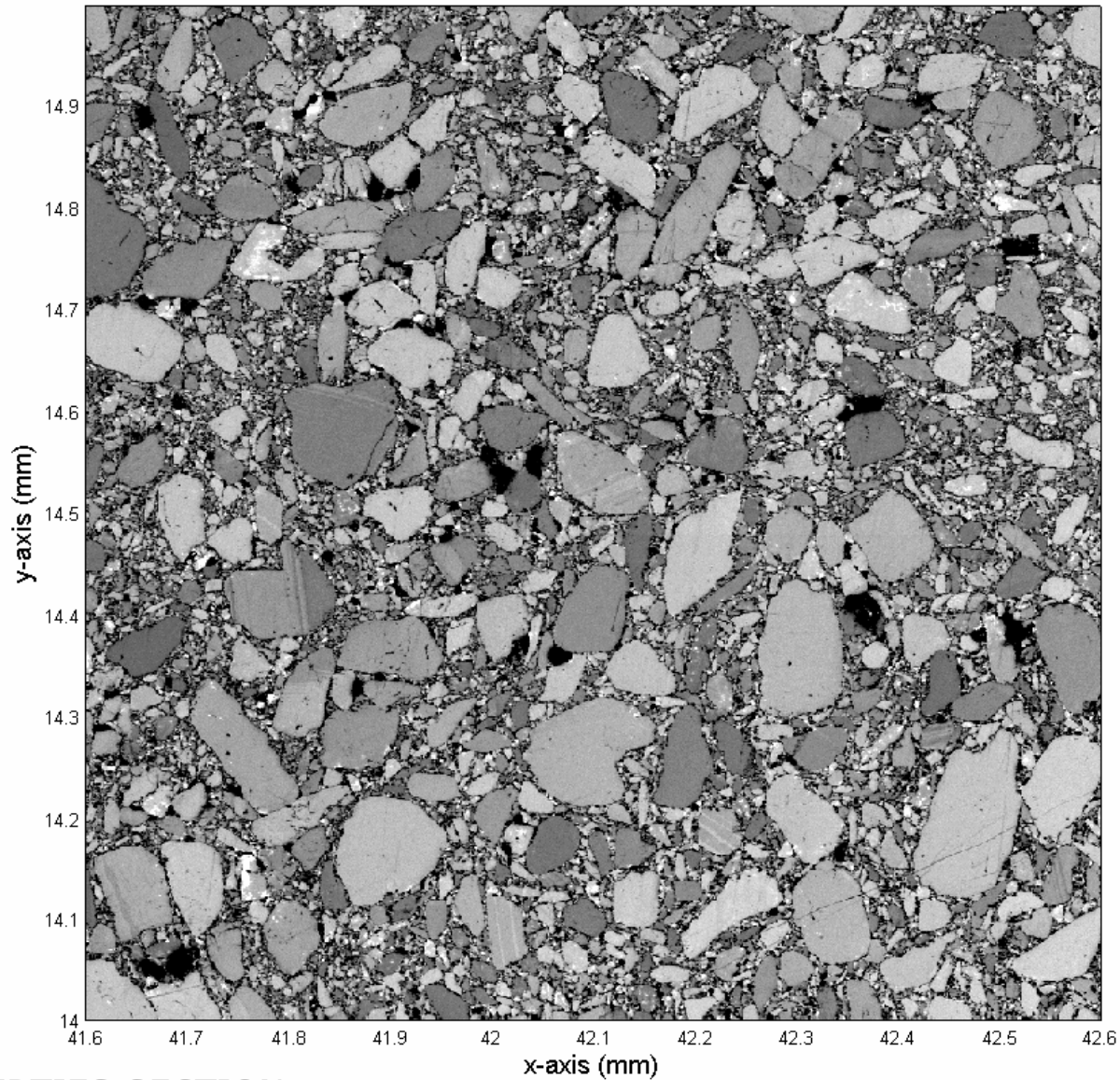
D M Williamson & Daniel Drodge

[dmw28@cam.ac.uk](mailto:dmw28@cam.ac.uk)

# Introduction

- Short introduction to PBXs
- Methods for thermal characterisation
- Methods for mechanical characterisation
- Methods for introducing controlled damage
- Evaluation of damaged materials

# Polymer Bonded Explosives



THERMAL PROPERTIES SECTION

# Thermal properties

# Thermal properties

Thermal diffusivity  $D$ , Conductivity  $\kappa$ , and Specific Heat  $C_P$  are all related by:

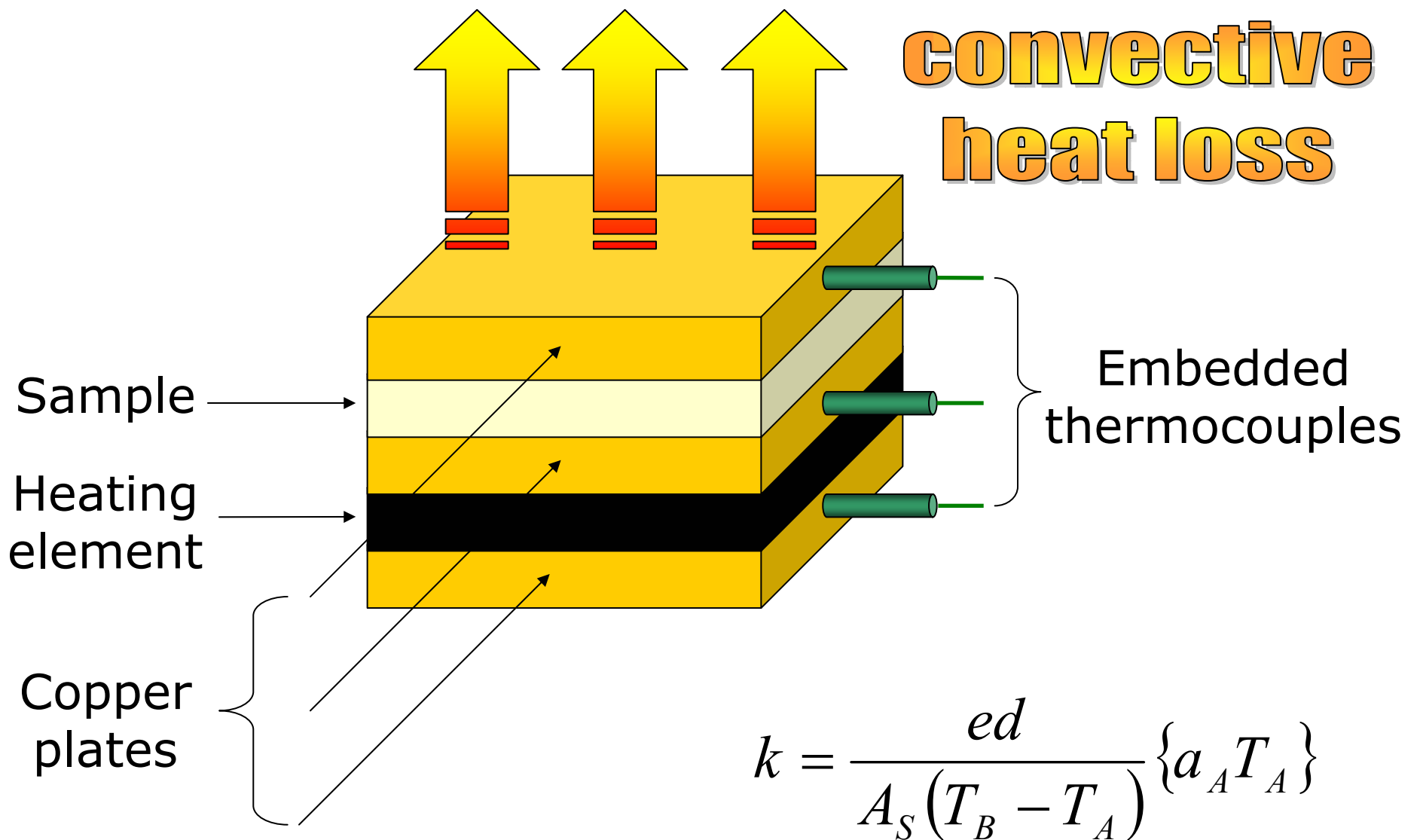
$$D = \frac{\kappa}{\rho C_P} , \quad (1)$$

We independently measured all three and used (1) to cross-check our result. Perform on PBXs and binder systems.

# Introduction

- Thermal conductivity via Lee's disc method:  
Temperature gradient across a sample analysed using Fourier's 1D heat flow equation.
- Thermal diffusivity via Ångström's method:  
Measure phase and amplitude evolution of a thermal wave propagating in a sample rod.
- Specific heat via DSC method:  
Power required to ramp temperature of sample a known amount is measured.
- Conductivity & diffusivity by transient hot-strip method:  
Due to Gustafsson *et al.* (1979) – solves heat equation for a heat source embedded in an 'infinite' body.

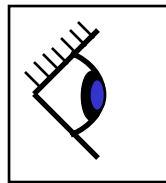
# Thermal conductivity



# Thermal diffusivity

$$D = \frac{Lv}{2 \ln(T_1 / T_2)}$$

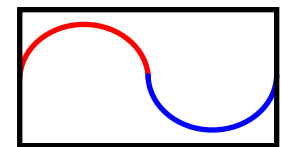
Thermal imaging camera (FLIR SC300)



Embedded thermocouples

Peltier cell

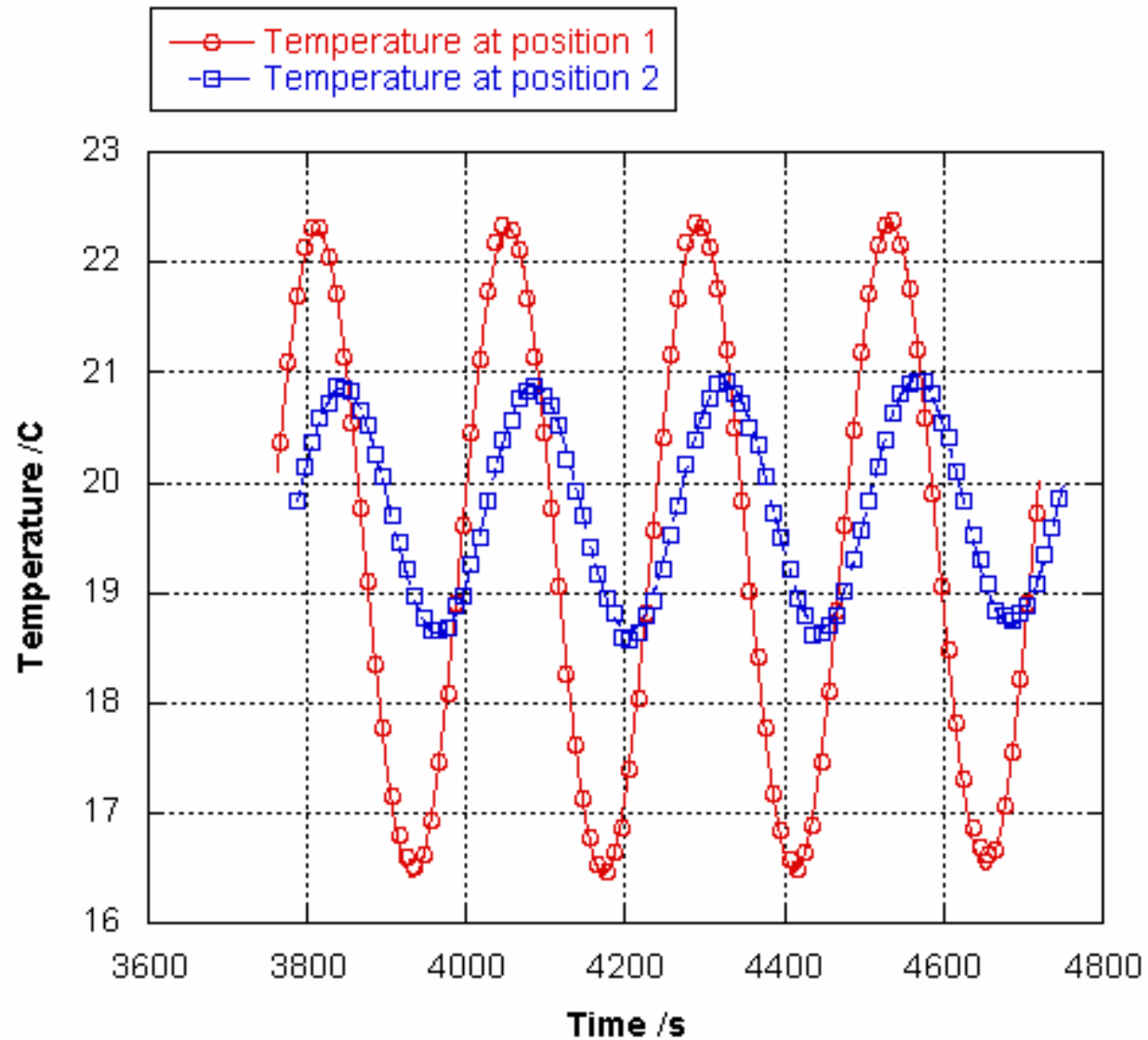
Water assisted copper heat exchanger



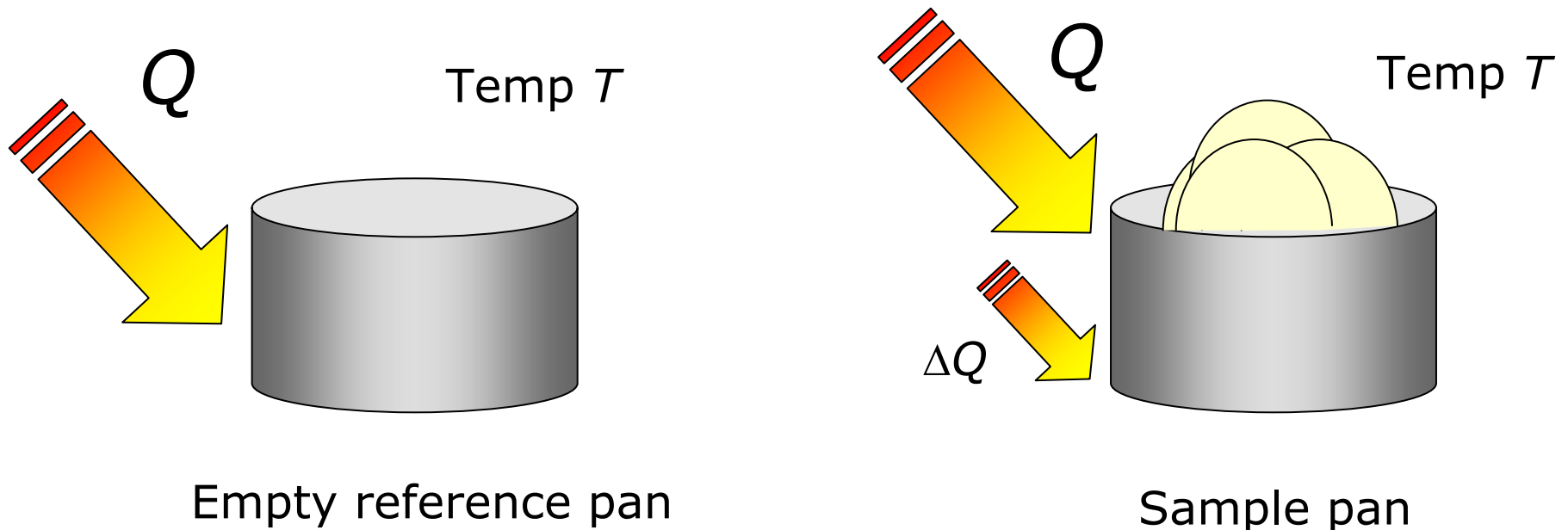
Water



# Thermal diffusivity



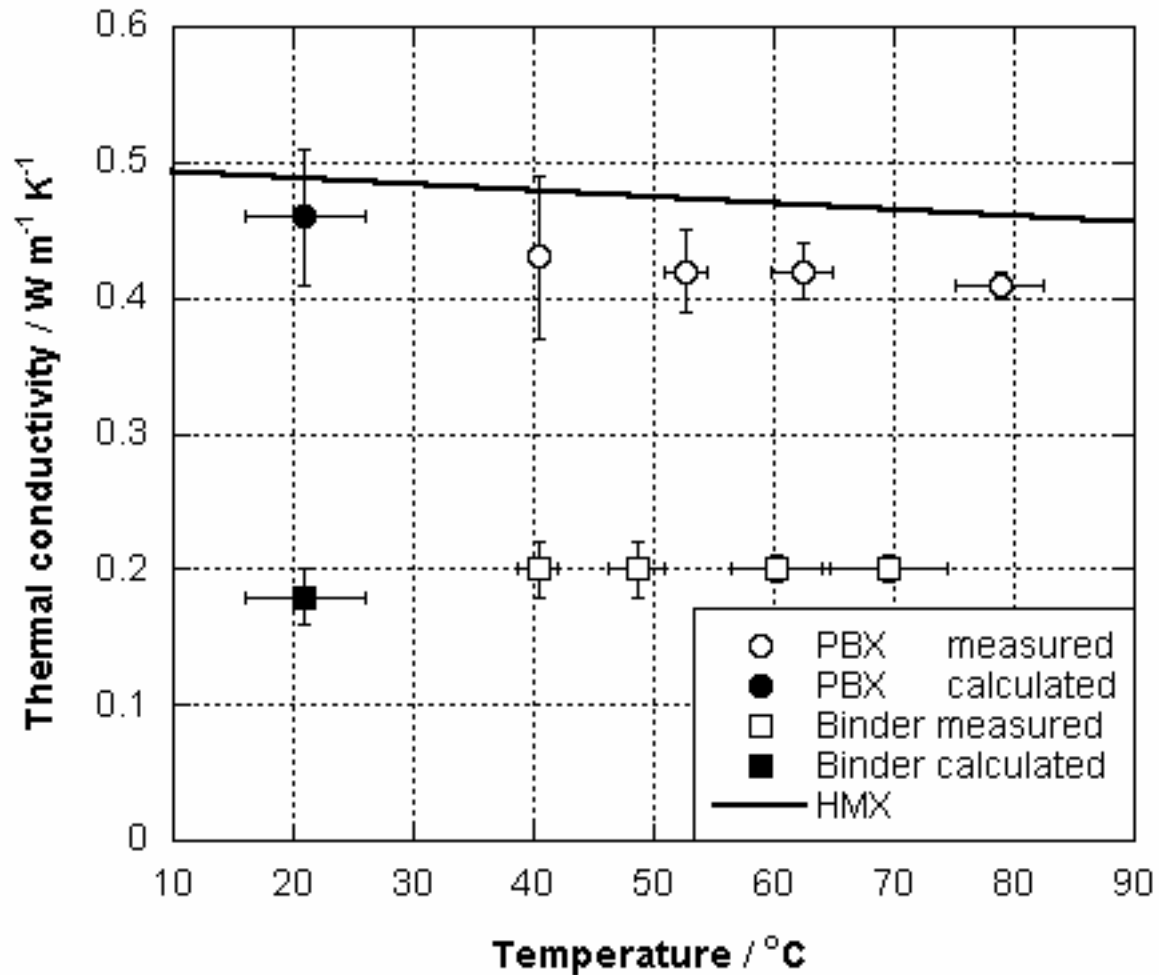
# Specific heat



Measure additional power required to keep both pans at same temperature during a temperature ramp:

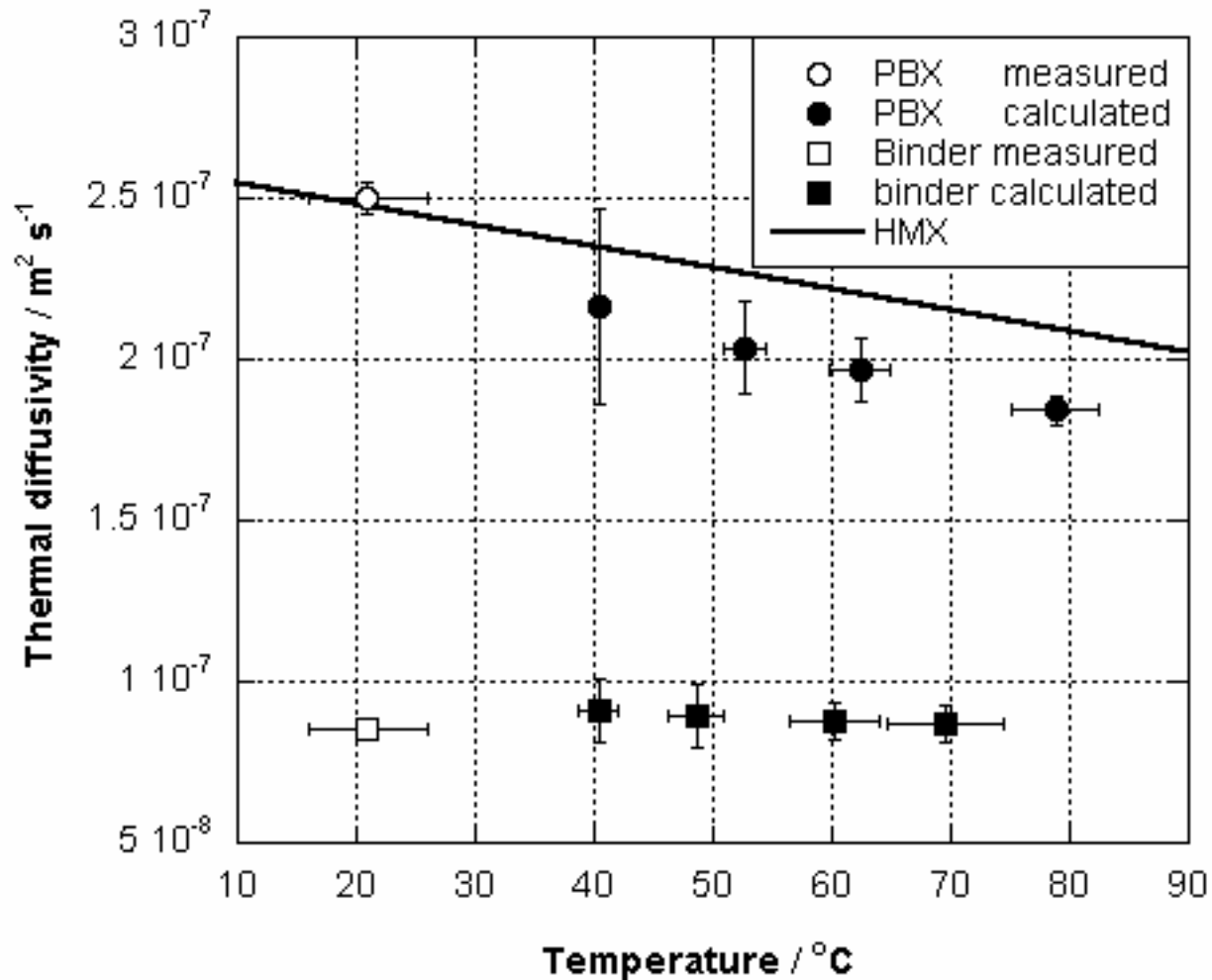
$$\frac{dQ}{dt} = mC_P \frac{dT}{dt}$$

# Thermal conductivity AWE PBX

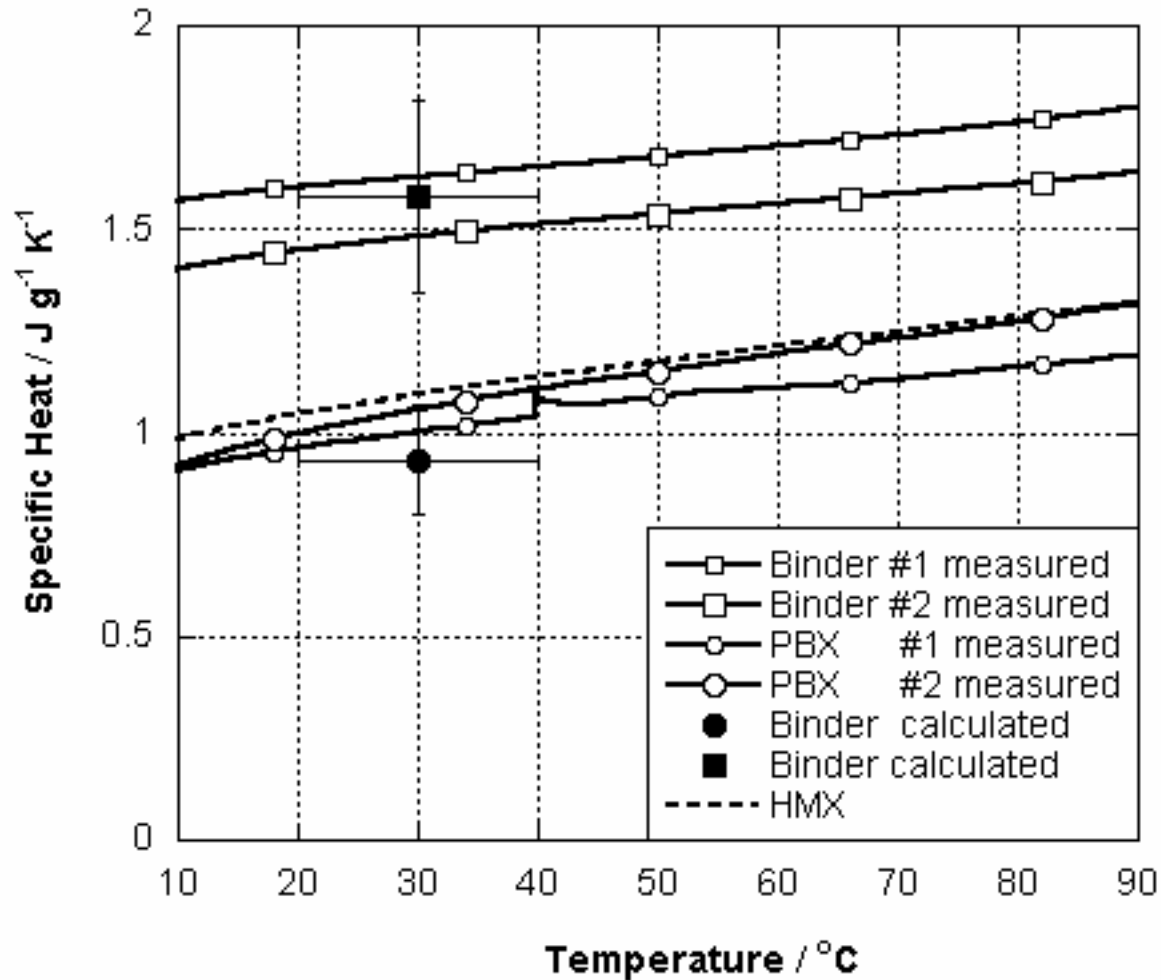


HMX data from: Hanson-Parr D.M., and Parr T.P. (1999)

# Thermal diffusivity AWE PBX



# Specific heat capacity AWE PBX

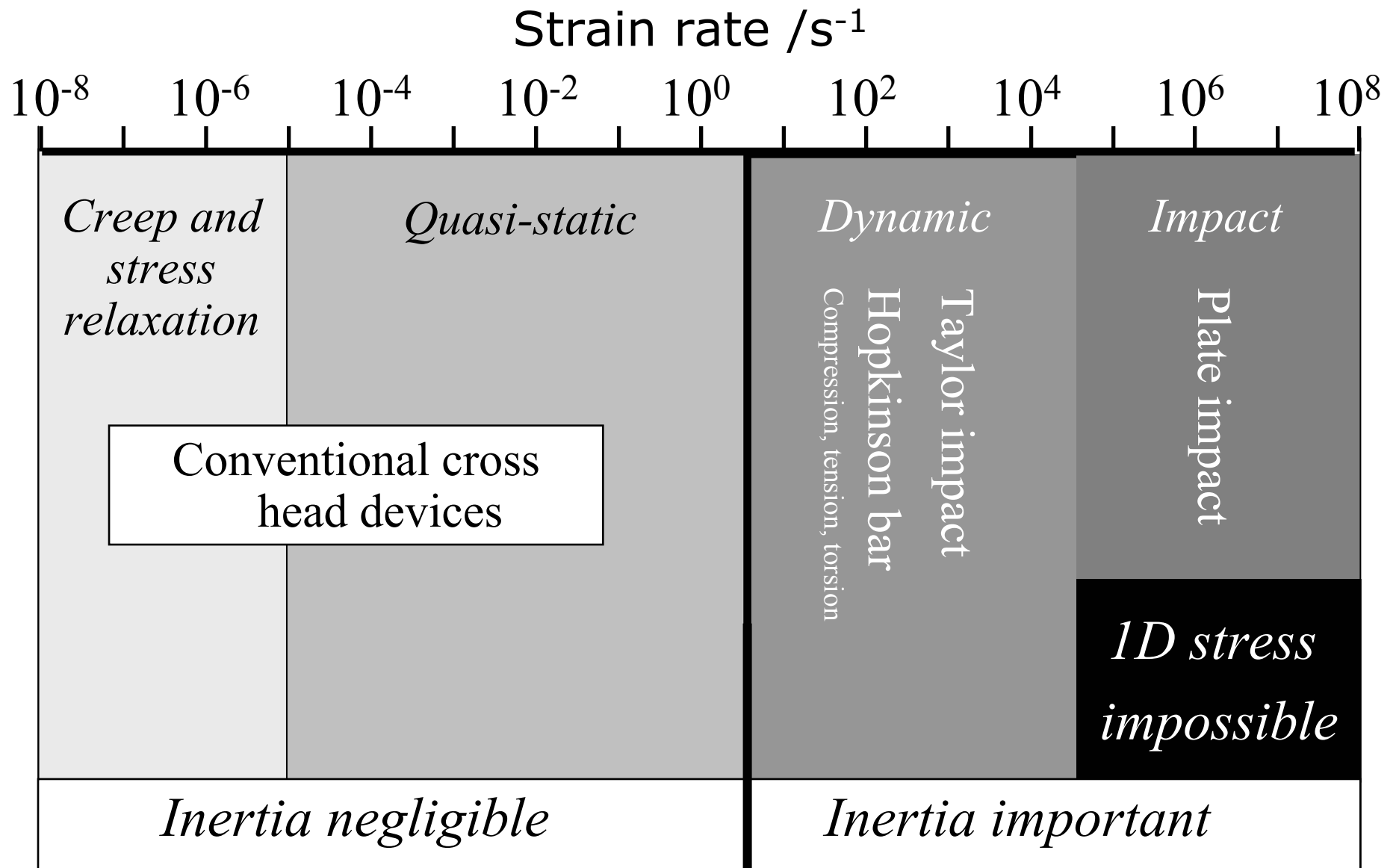


Large 'error' on temperature due to diffusivity data at 20°C and conductivity data at 40°C

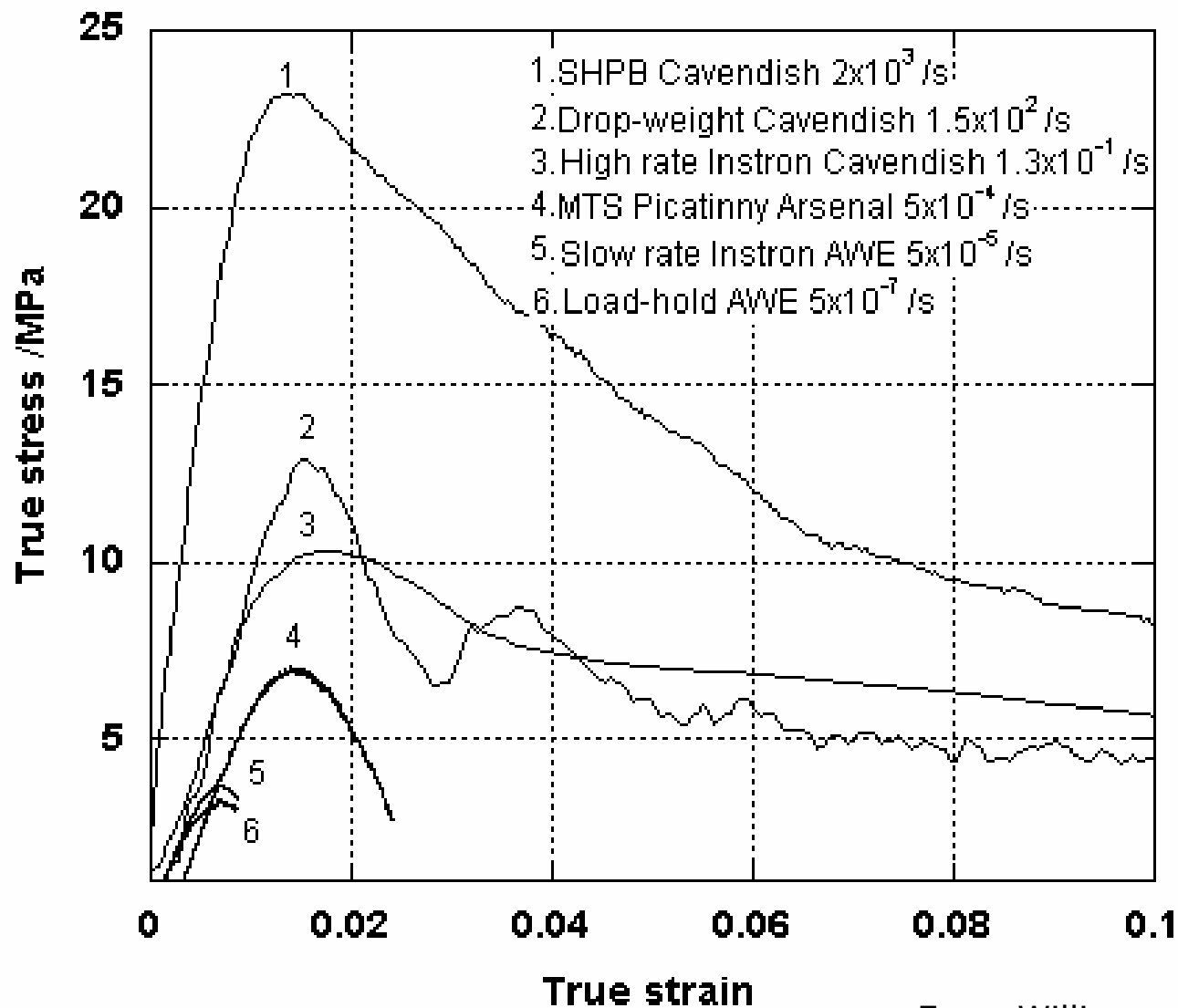
# Mechanical Properties

STRAIN RATES OF INTEREST

# Strain rates of interest

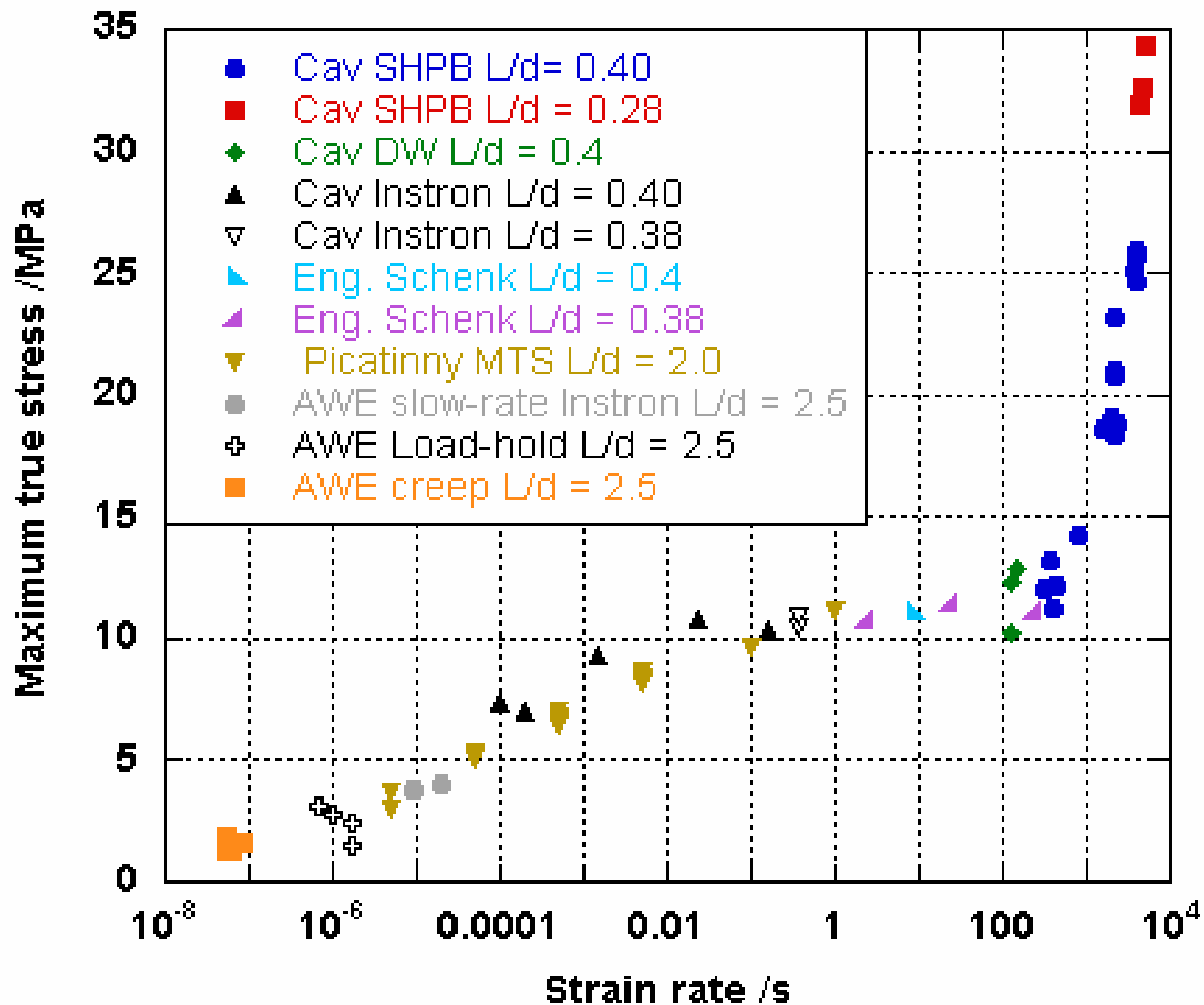


# Rate dependence of AWE PBX

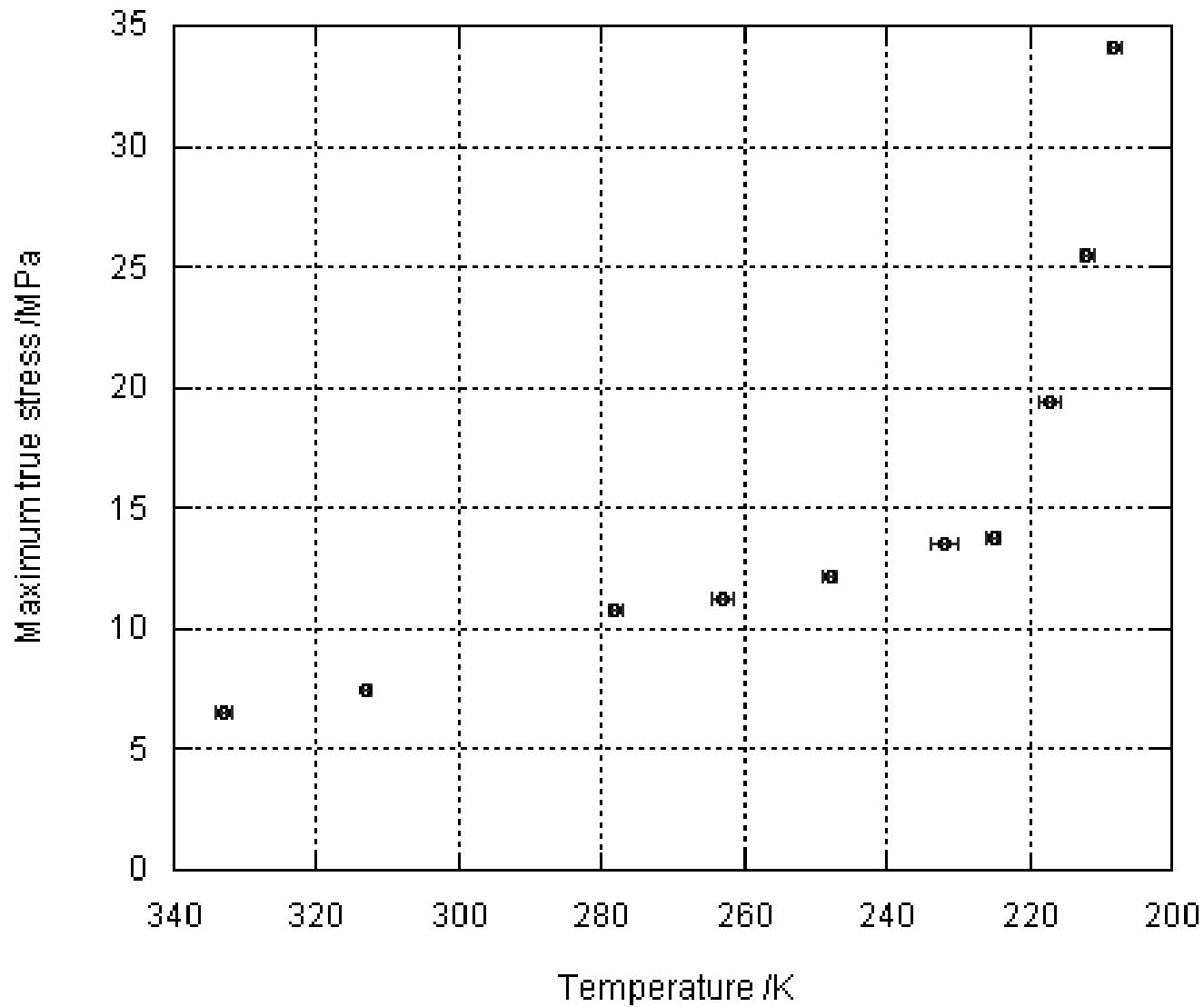




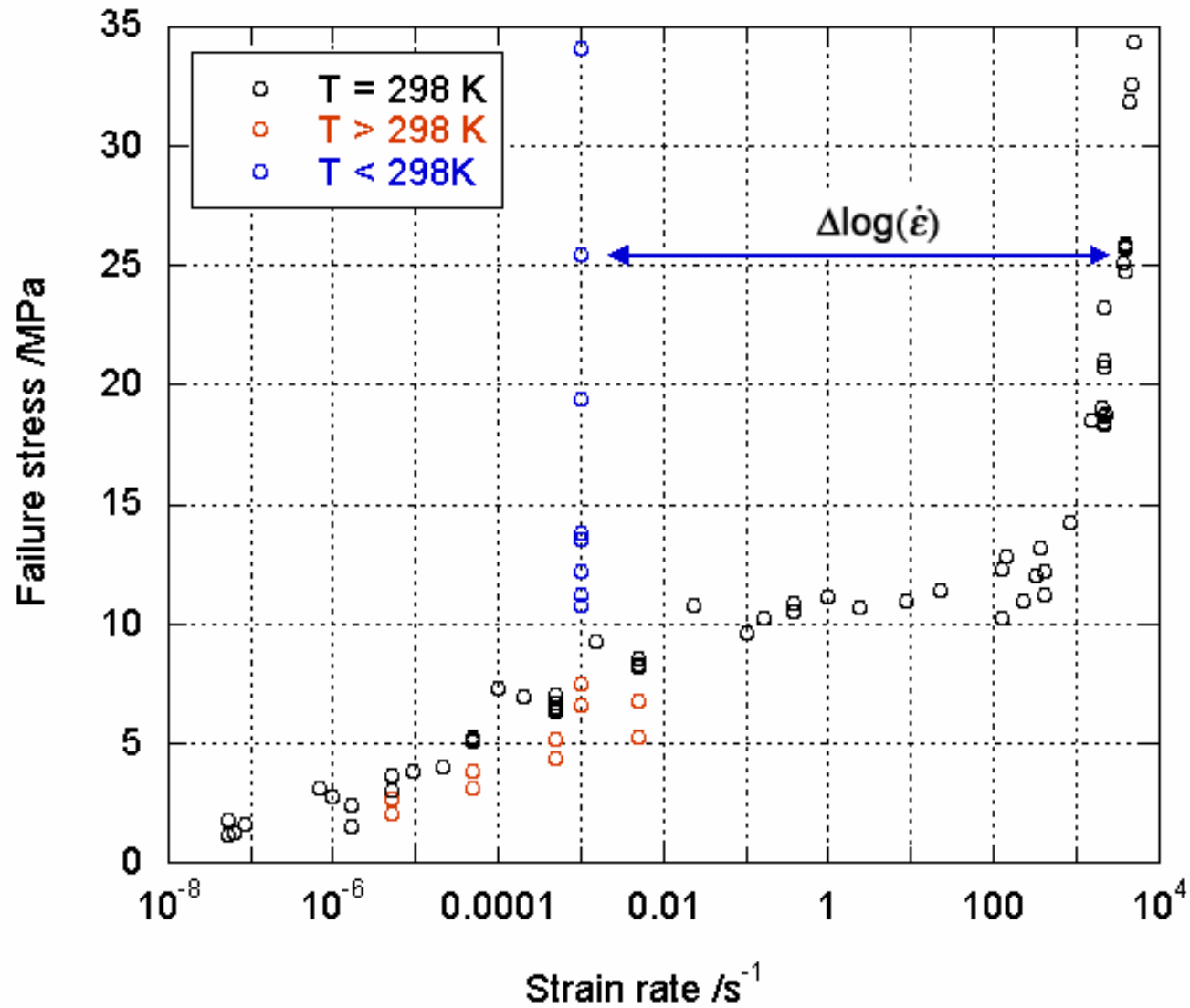
# Rate dependence of AWE PBX



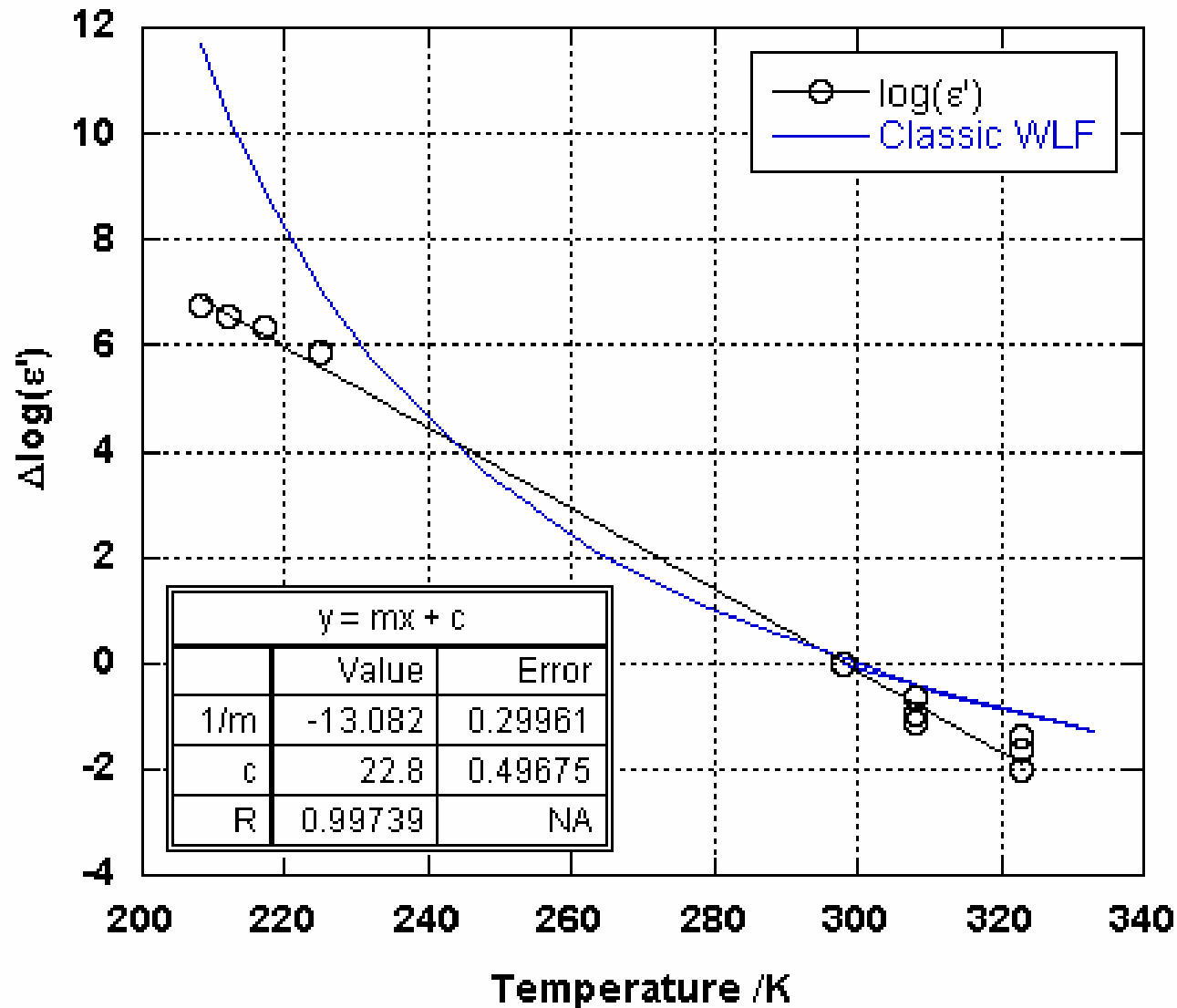
# Temperature dependence of AWE PBX



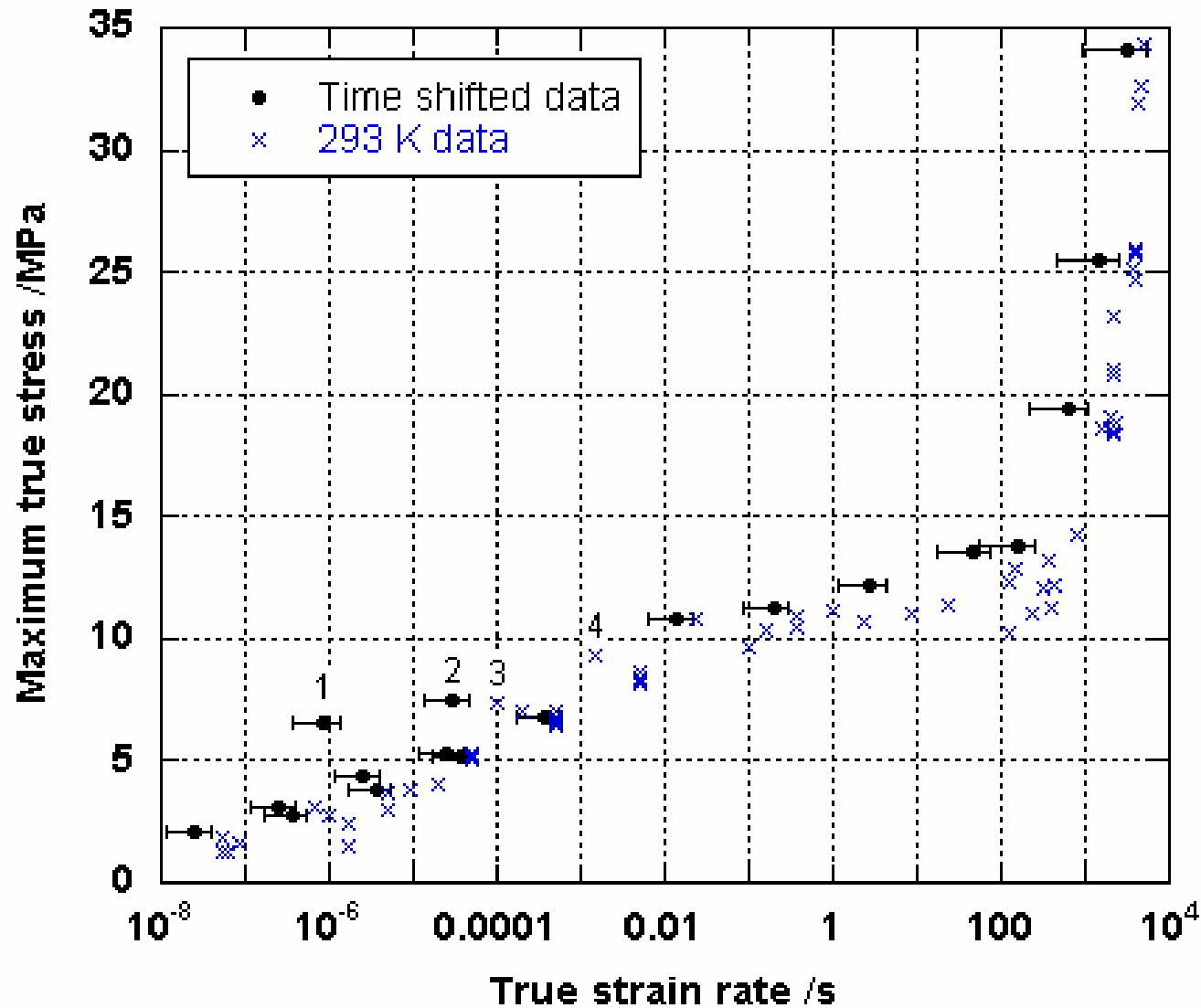
# Temperature-Rate dependence of AWE PBX



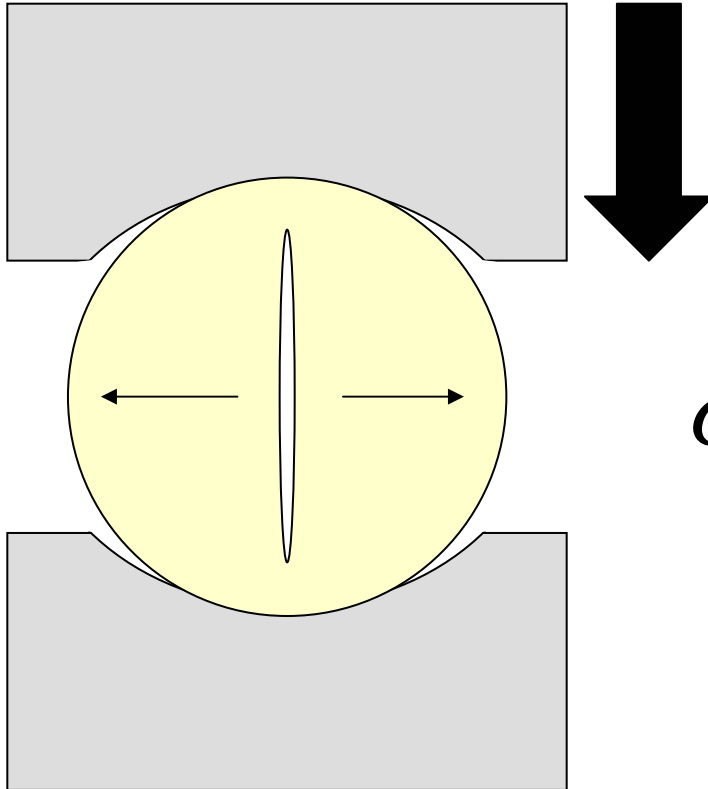
# Temperature-Rate dependence of AWE PBX



# Temperature-Rate dependence of AWE PBX



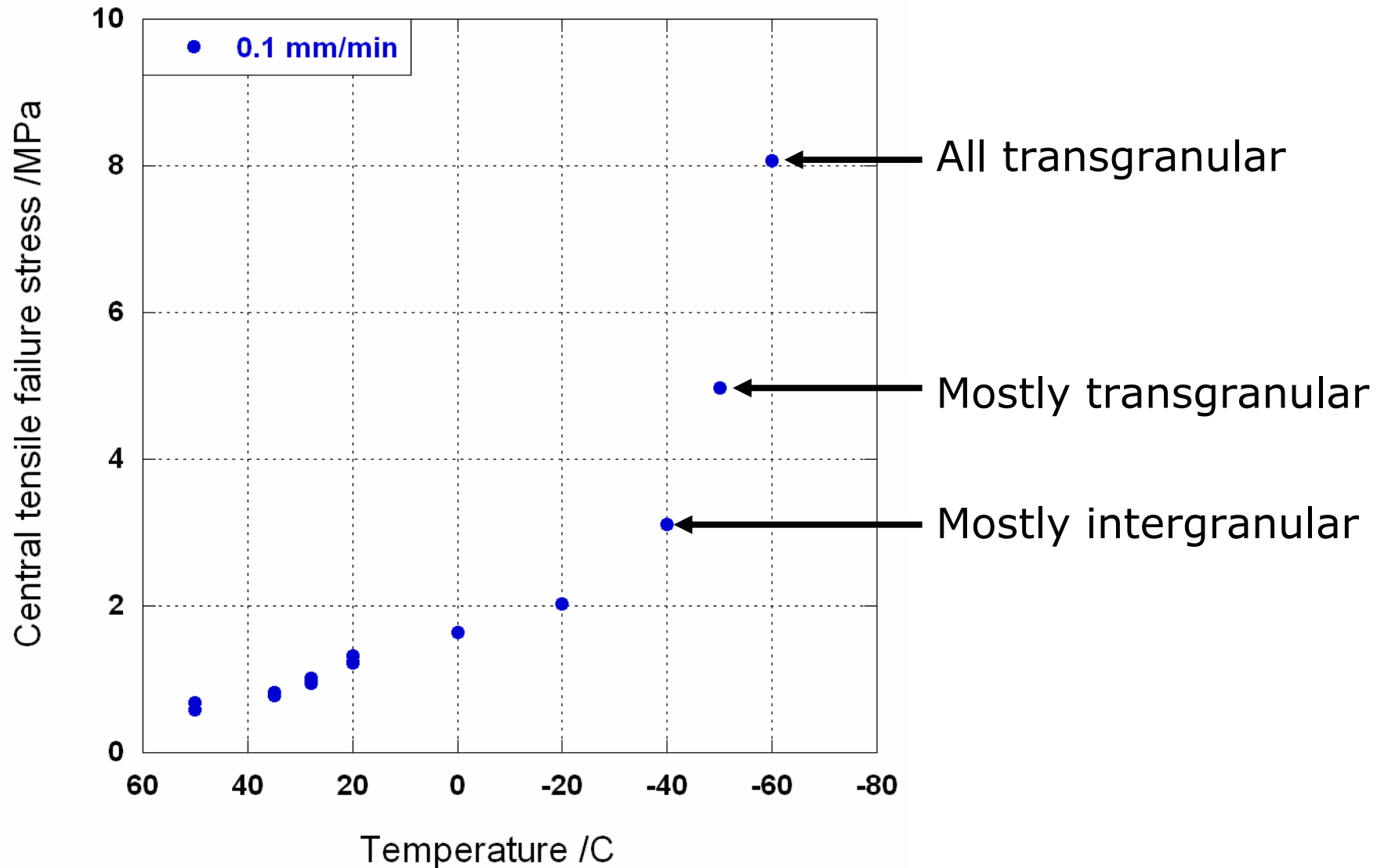
# Brazilian test



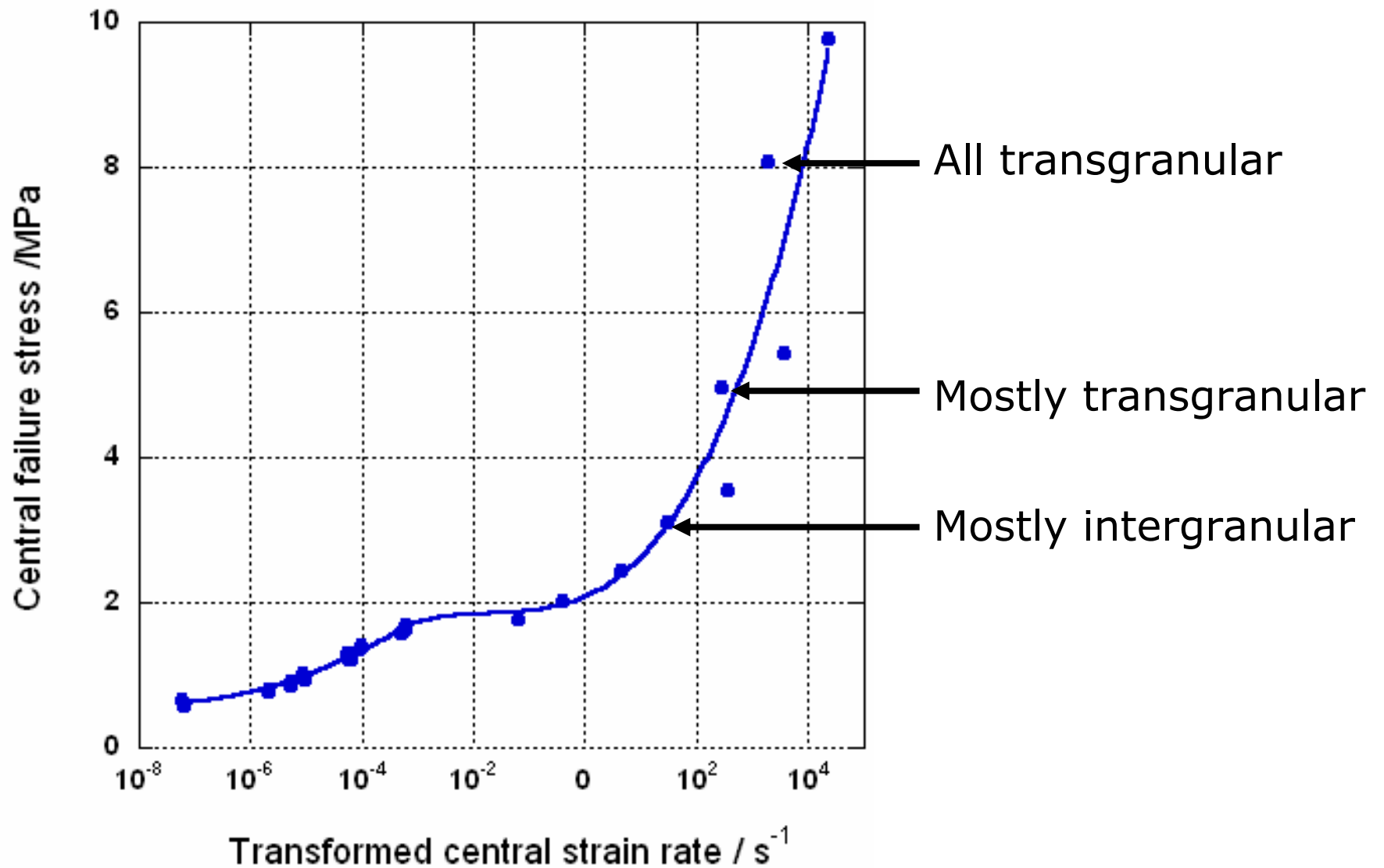
$$\sigma_F = \frac{2P}{\pi DT} \left( 1 - \left( \frac{b}{R} \right)^2 \right)$$

Brazilian test

# Failure mode AWE PBX

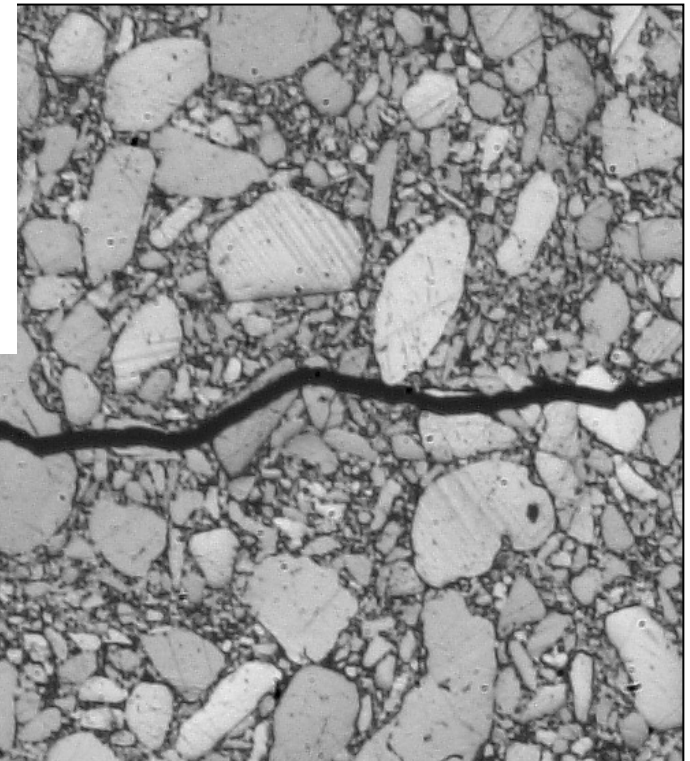
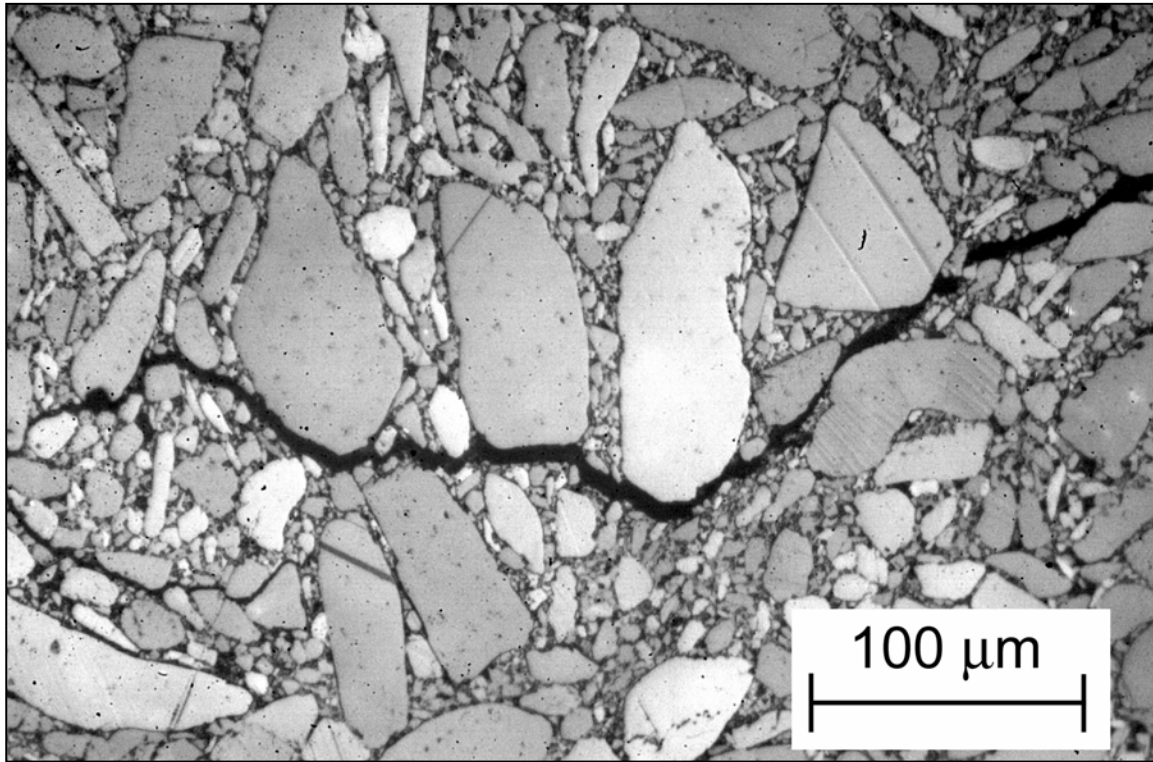


# Failure mode AWE PBX





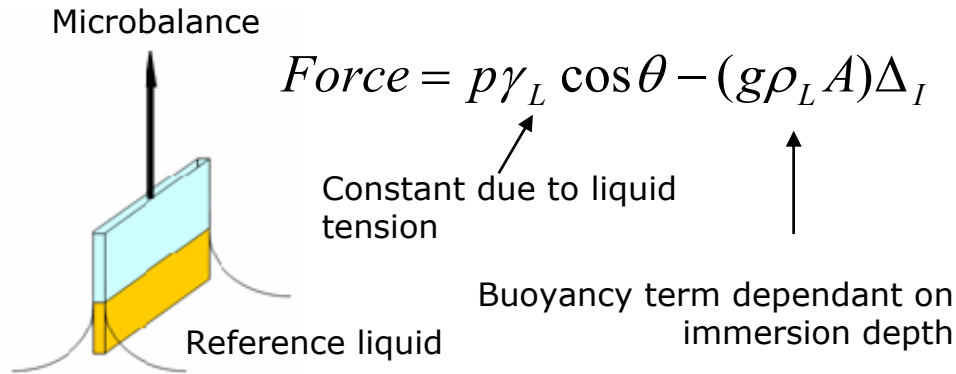
# A different response?



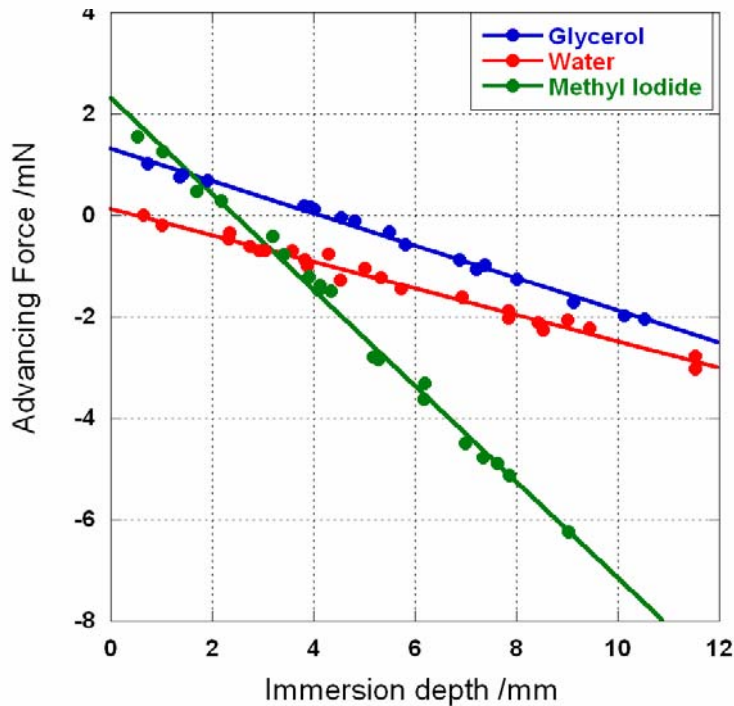
From Williamson *et al.* (2009a)

THERMO ADHESION

# Thermodynamic Work of Adhesion



The Wilhelmy plate method was used; Rosano *et al.* (1971). Binder coated microscope slides were immersed in reference liquids. The resultant push/pull due to surface buoyancy/tension was measured.



Work of adhesion  $W_a$  between liquid of surface tension  $\gamma_L$  which forms a perimeter  $p$  of contact angle  $\theta$  against the binder is related to the measured force  $f$  by

$$W_a = \gamma_L + f/p = \gamma_L + \gamma_L \cos\theta$$

In analysis due to Kaelble (1970) the interactions of a non-fully-wetting liquid on a solid surface is described by:

$$W_a = 2\sqrt{(\gamma_L^d \gamma_S^d)} + 2\sqrt{(\gamma_L^P \gamma_S^P)}$$

Simultaneous equations using liquid pairs: solve for binder surface energy components

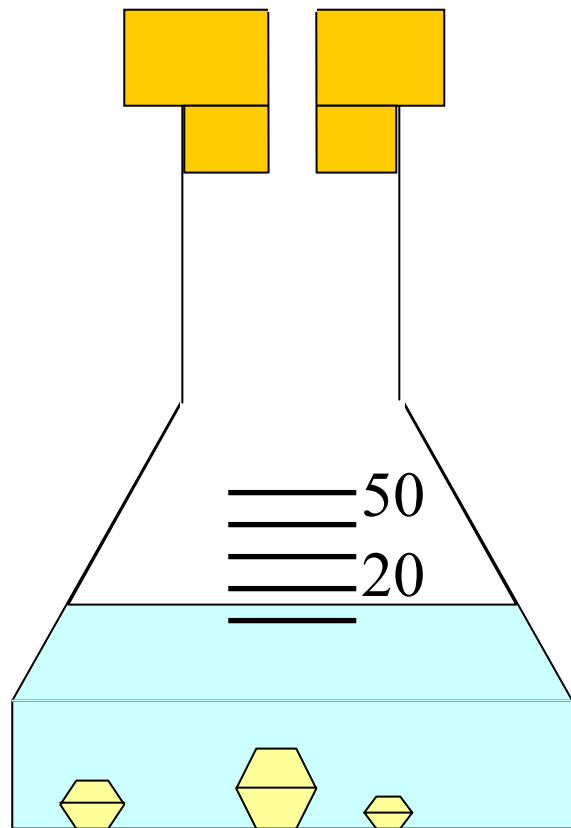
From Williamson *et al.* (2009b)

# Thermodynamic Work of Adhesion

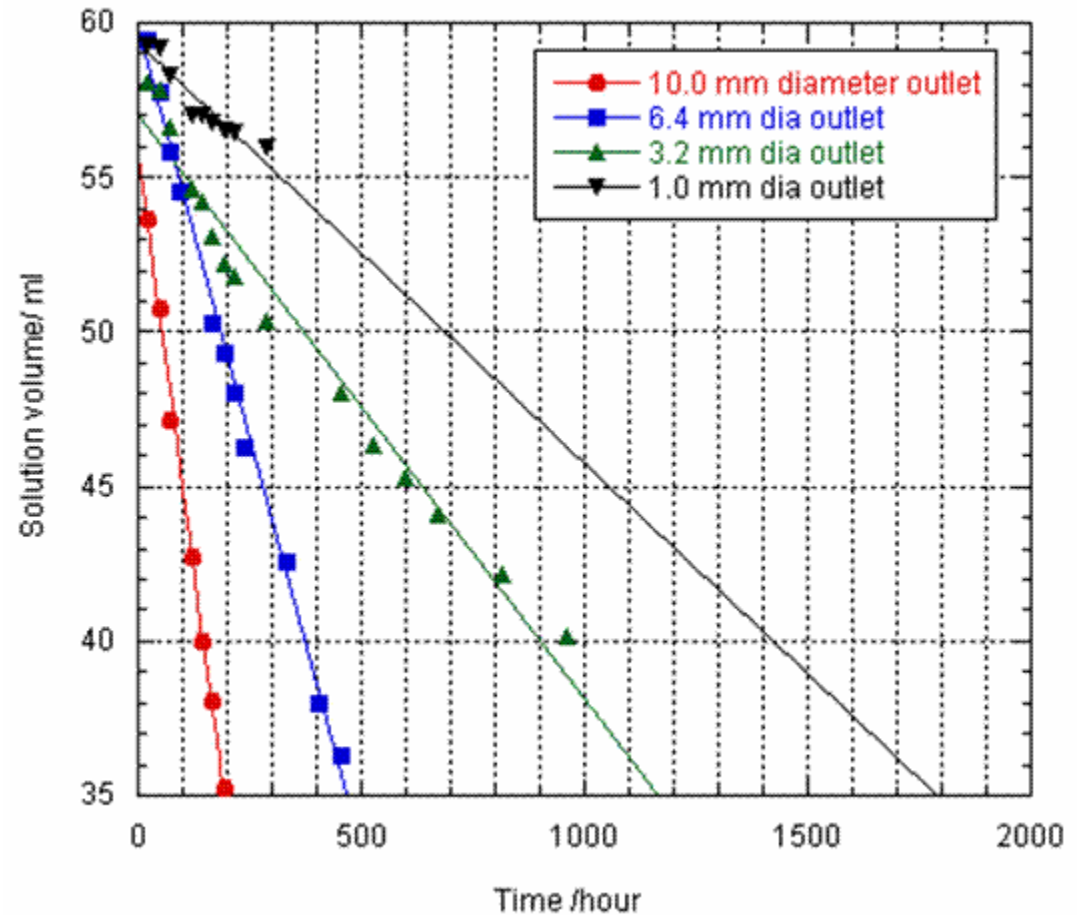
From these data and analyses the surface energy of the coating can be inferred ( $42.5 \pm 2.8 \text{ mJ/m}^2$ ), and when combined with HMX data (Yee *et al.* 1980), the TWA calculated.

<b>Crystal Face</b>	<b>HMX surface energy /mJ/m<sup>2</sup></b>	<b>HMX – binder TWA /mJ/m<sup>2</sup></b>
{011}	45.0	$81.5 \pm 6.5$
{010}	46.0	$78.8 \pm 7.9$
{110}	48.0	$79.7 \pm 8.3$

# Measured Work of Adhesion: crystals

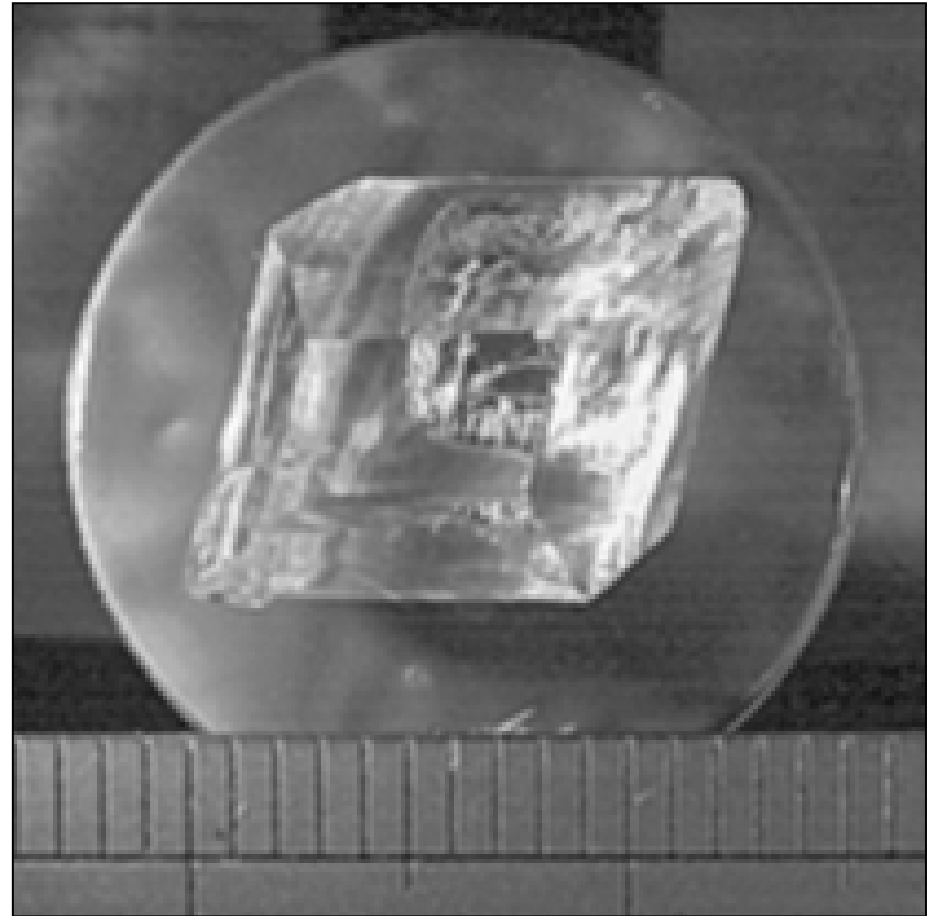
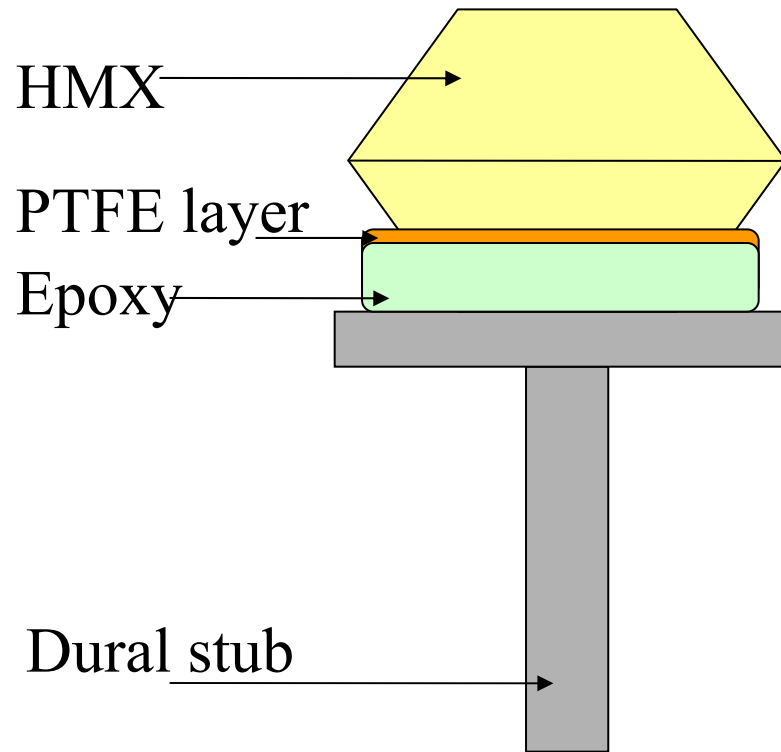


Growth by evaporation



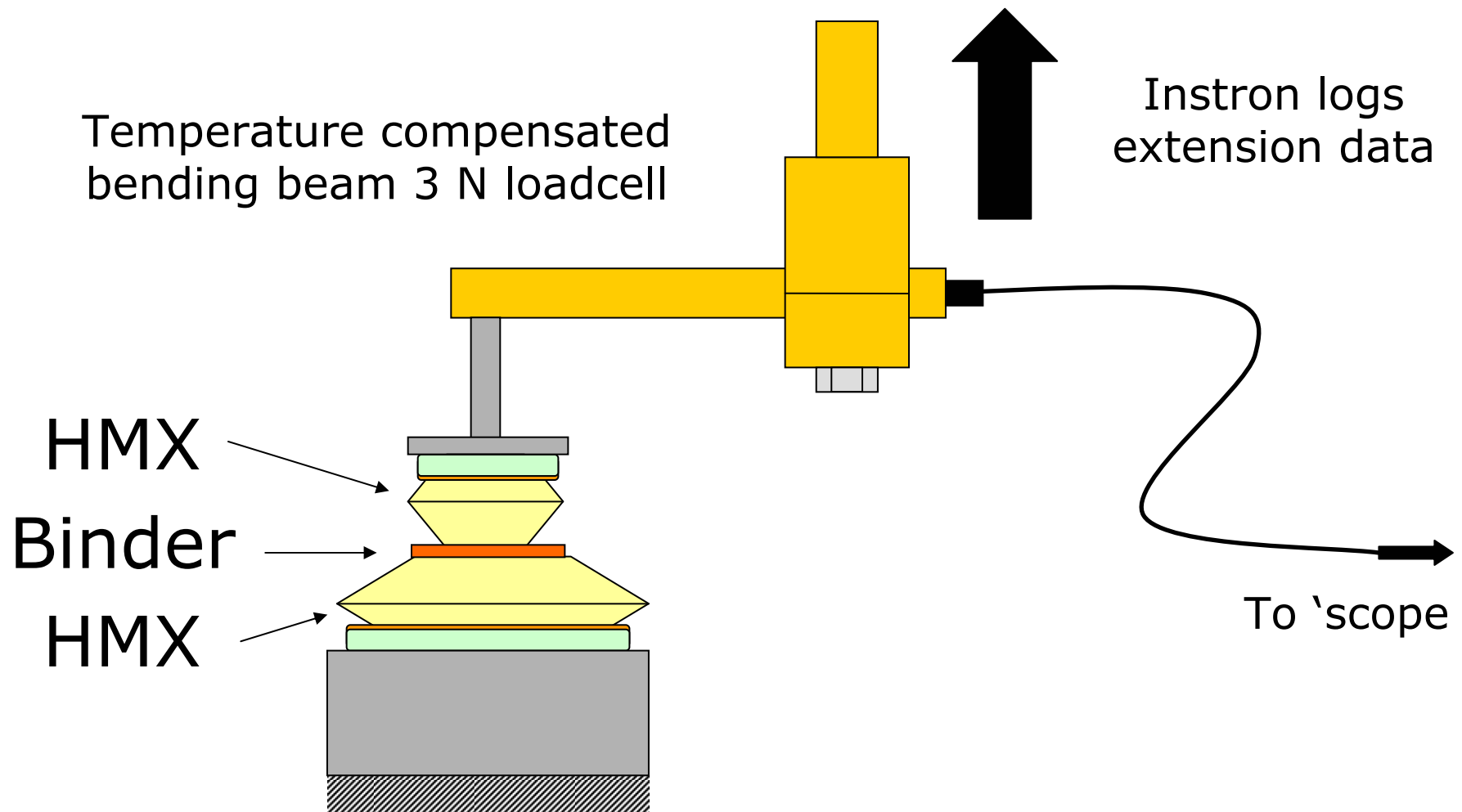
Controlled growth rate for 'best' crystals

# Experimental procedure: crystal

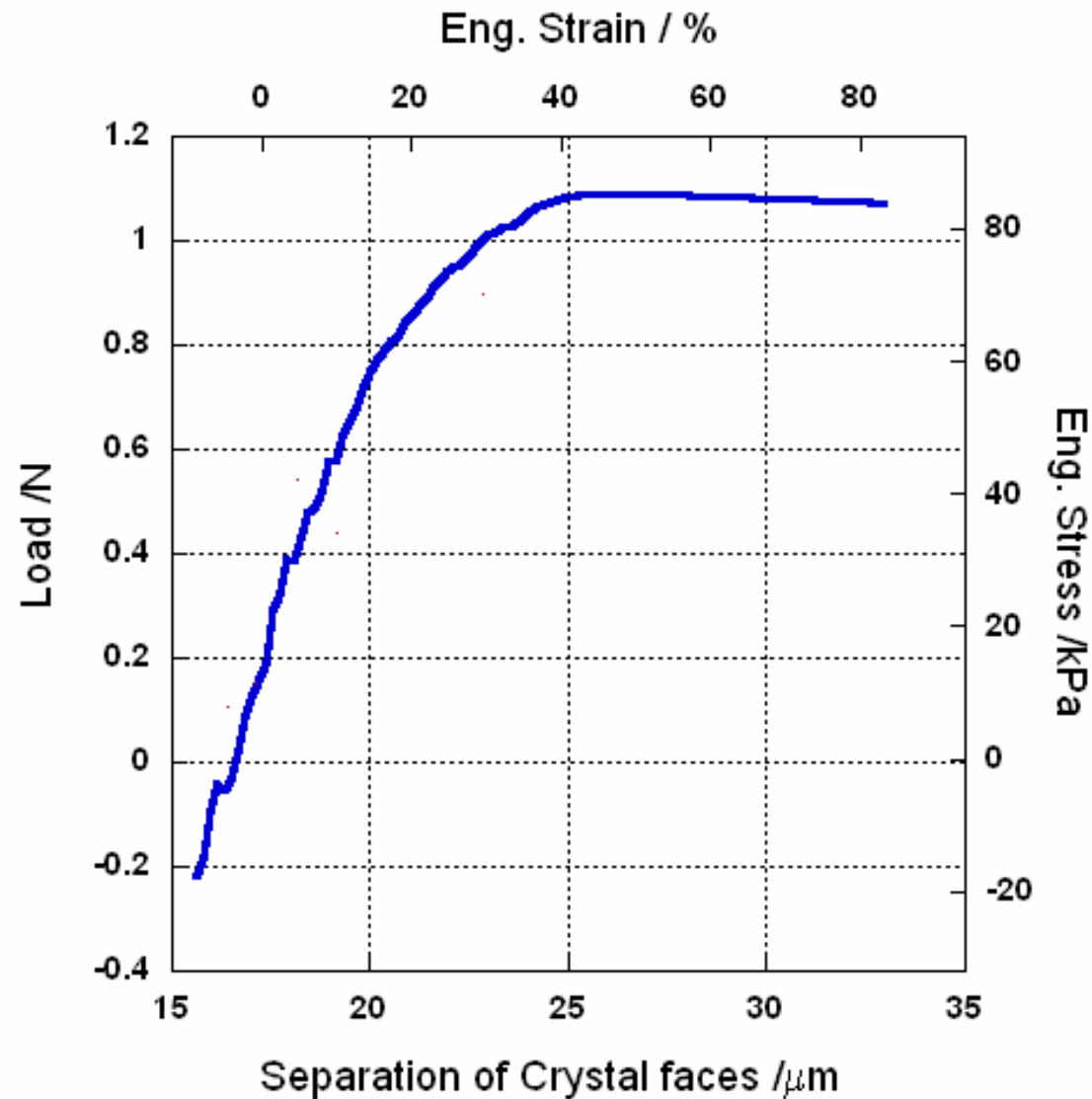


Single crystals  $\sim 1 \text{ cm}^3$

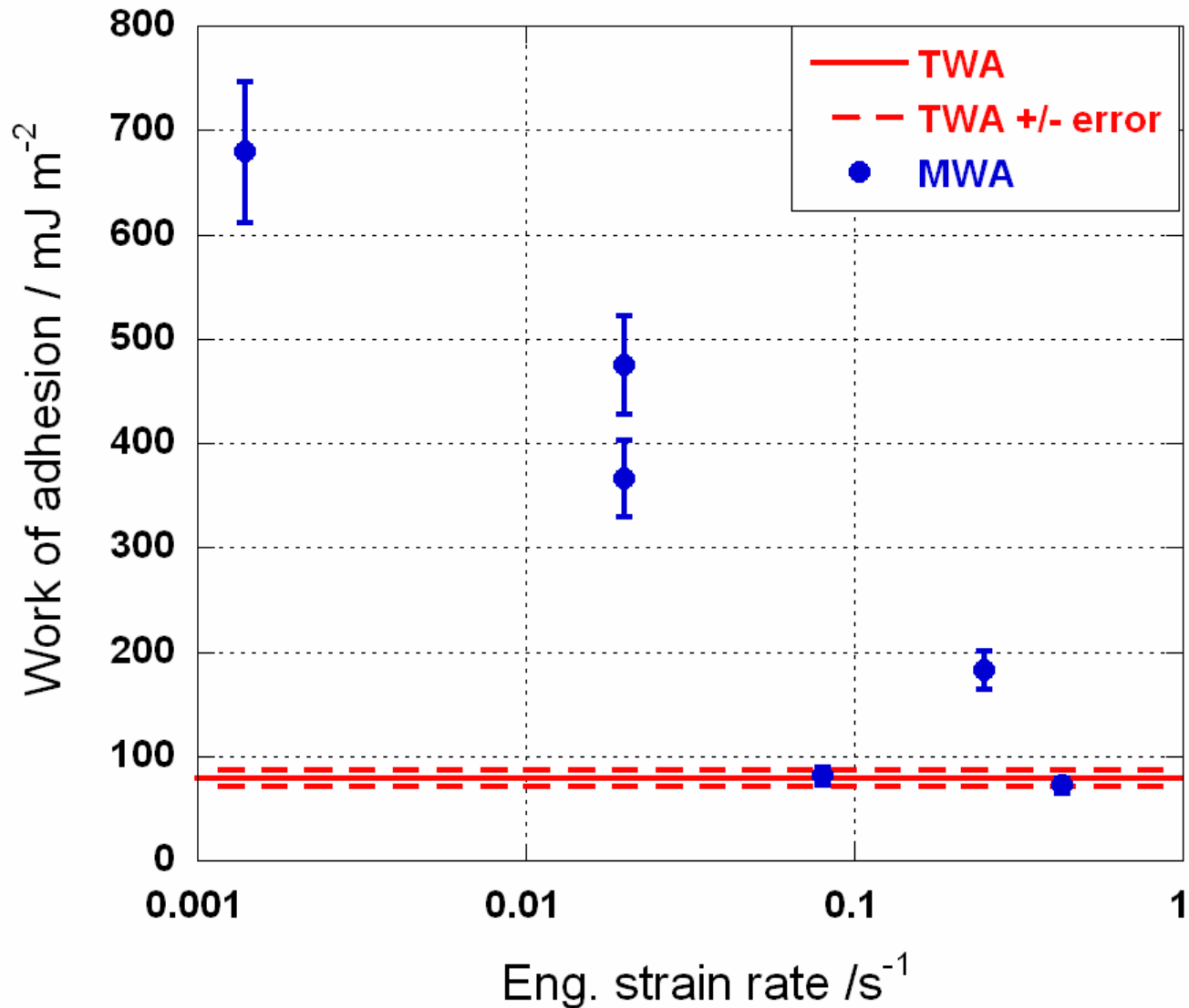
# Measured Work of Adhesion : loadcell



# Measured Work of Adhesion

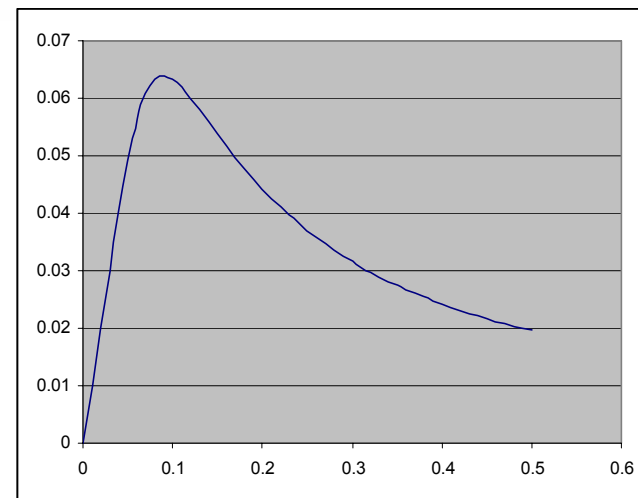
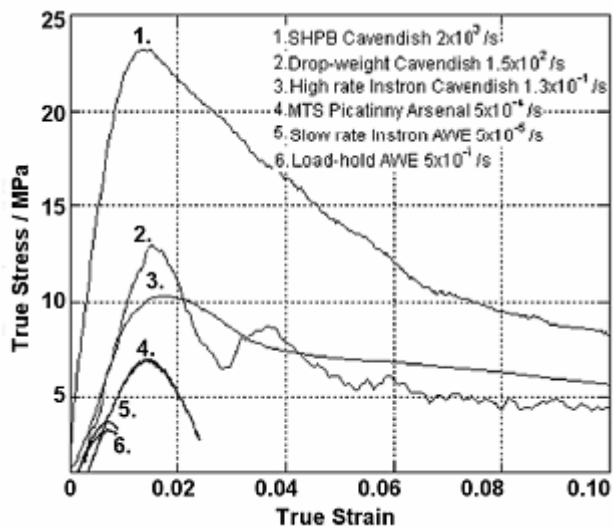
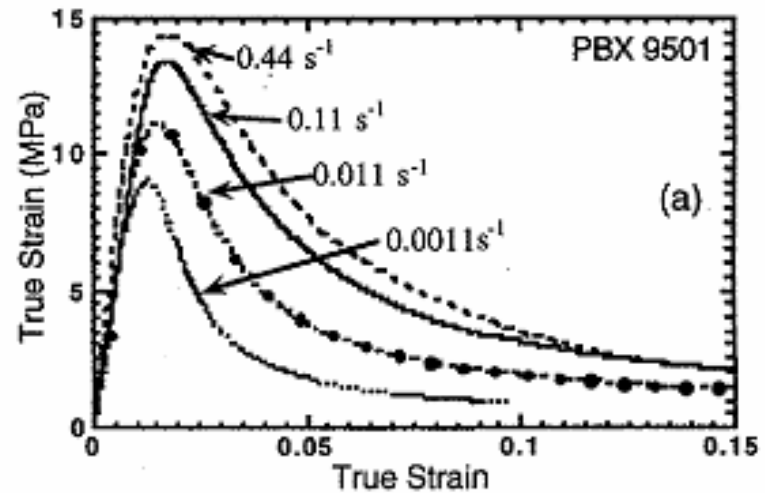
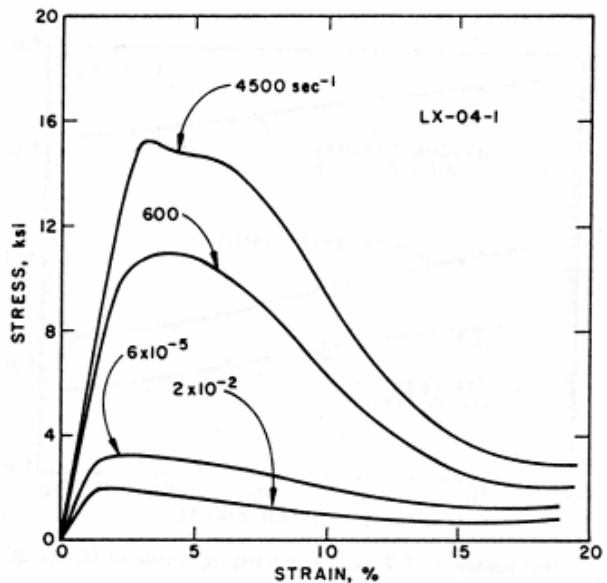


# Work of Adhesion





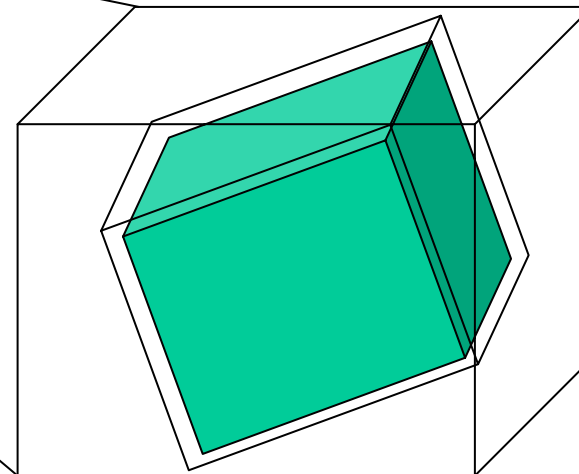
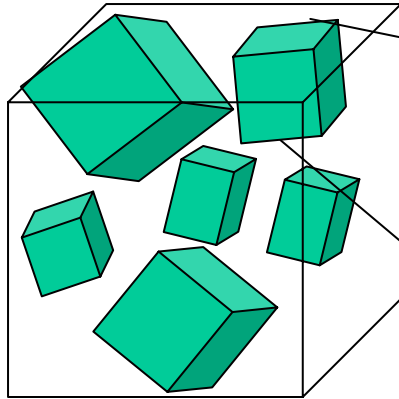
# A description of failure



$$\sigma(\varepsilon) = M_0 \varepsilon (1 - \exp(-\varepsilon_a^2 / \varepsilon^2))$$

Simple model of adhesion

# Based on a simple model



Local Volume:  $V$   
Global Strain:  $\varepsilon$   
Local Modulus:  $M_0$   
Particle Surface Area:  $A$   
Surface Energy:  $\gamma$

$$\text{Debond Energy} = A\gamma$$

$$\begin{aligned}\text{Strain Energy} &= \frac{1}{2}M_0\varepsilon^2 \\ \varepsilon_a^2 &= 2A\gamma / M_0V\end{aligned}$$

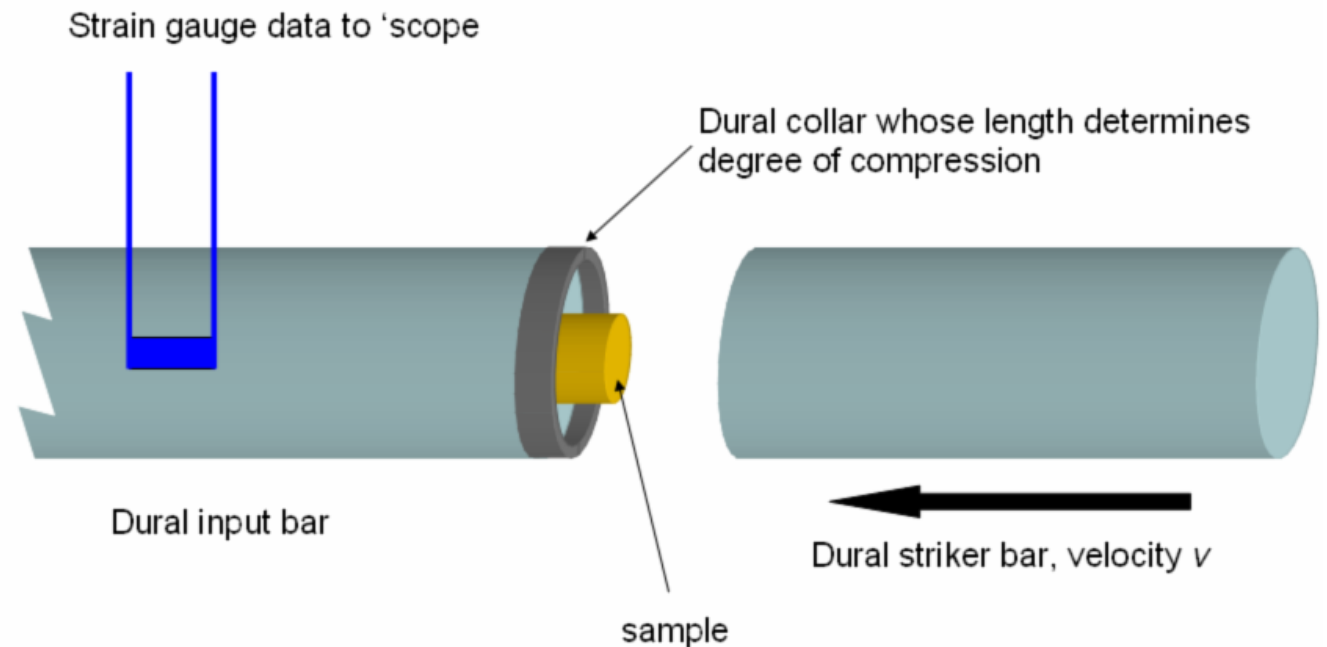
# Inducing controlled damage

# QRXs QinetiQ Research eXplosives

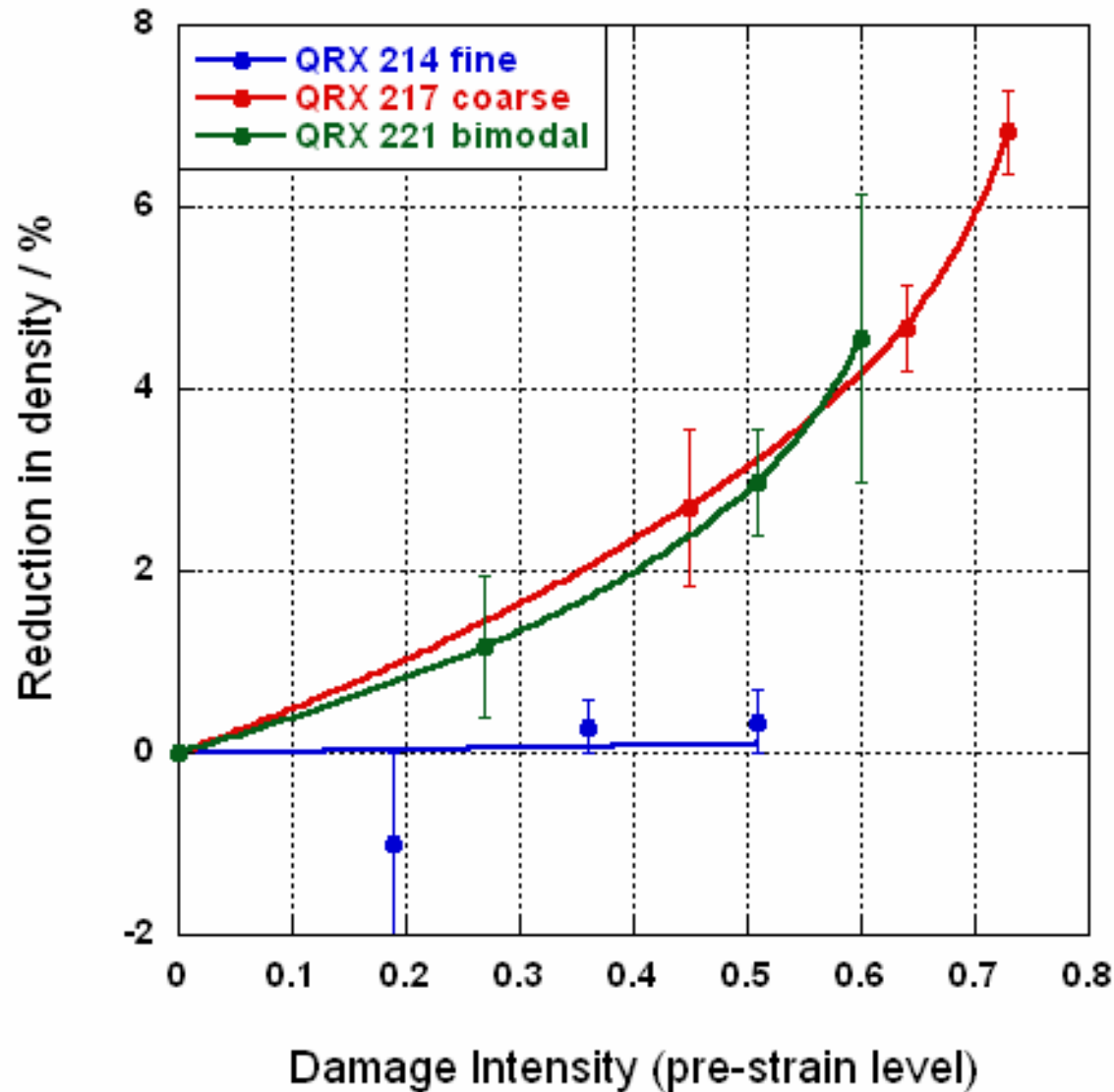
Constituent	Material and mass fractions		
	QRX 214	QRX 221	QRX 217
RDX	0.75	0.80	0.70
HTPB based binder	0.15	0.20	0.30
Density g/cm <sup>3</sup>	1.455	1.517	1.426
Particle size distribution	Monomodal fine	Bimodal ↔	Monomodal coarse

# Inducing controlled damage

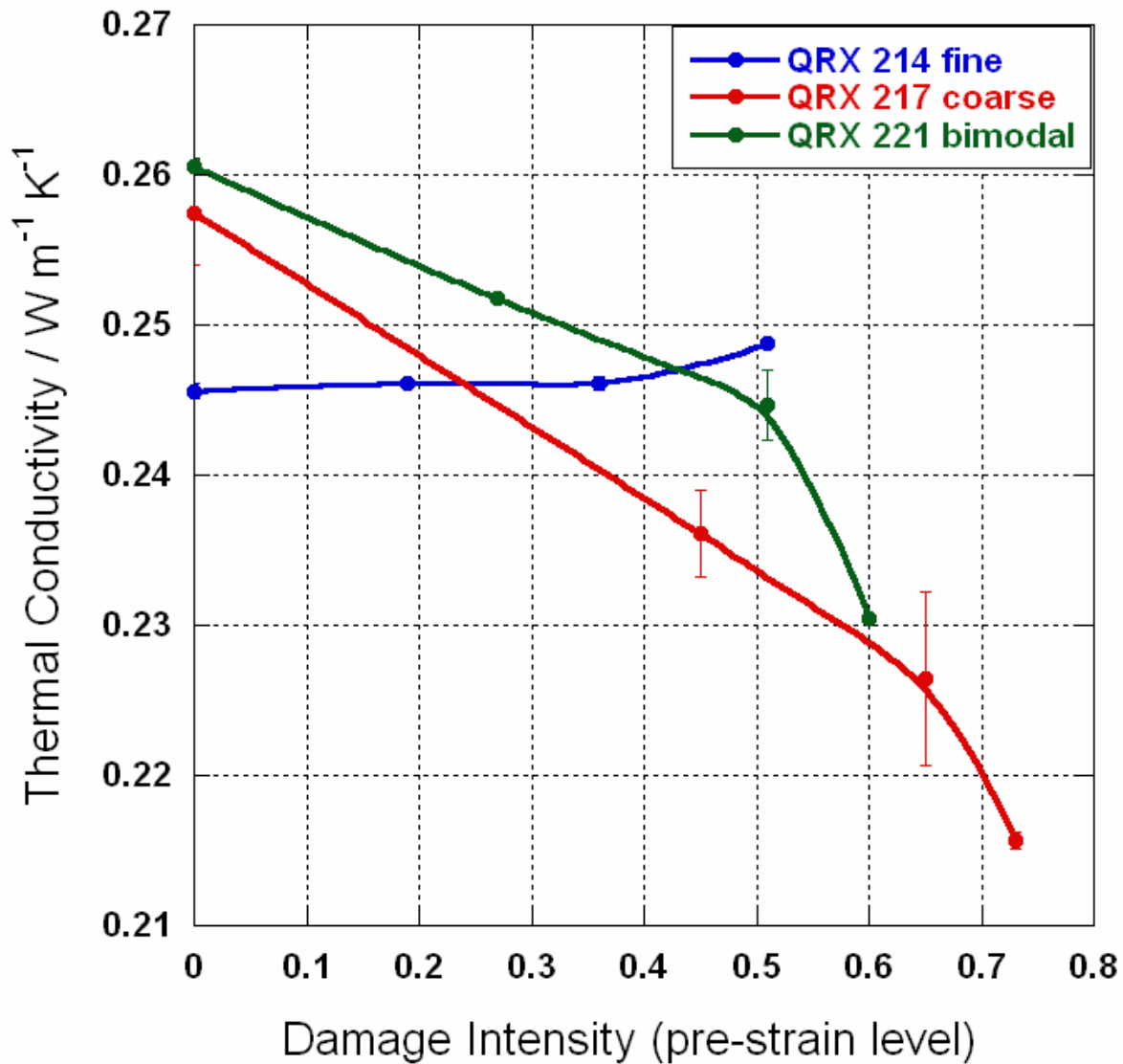
A restricted stroke SHPB or drop-weight is used to dynamically compress a pre-determined amount.



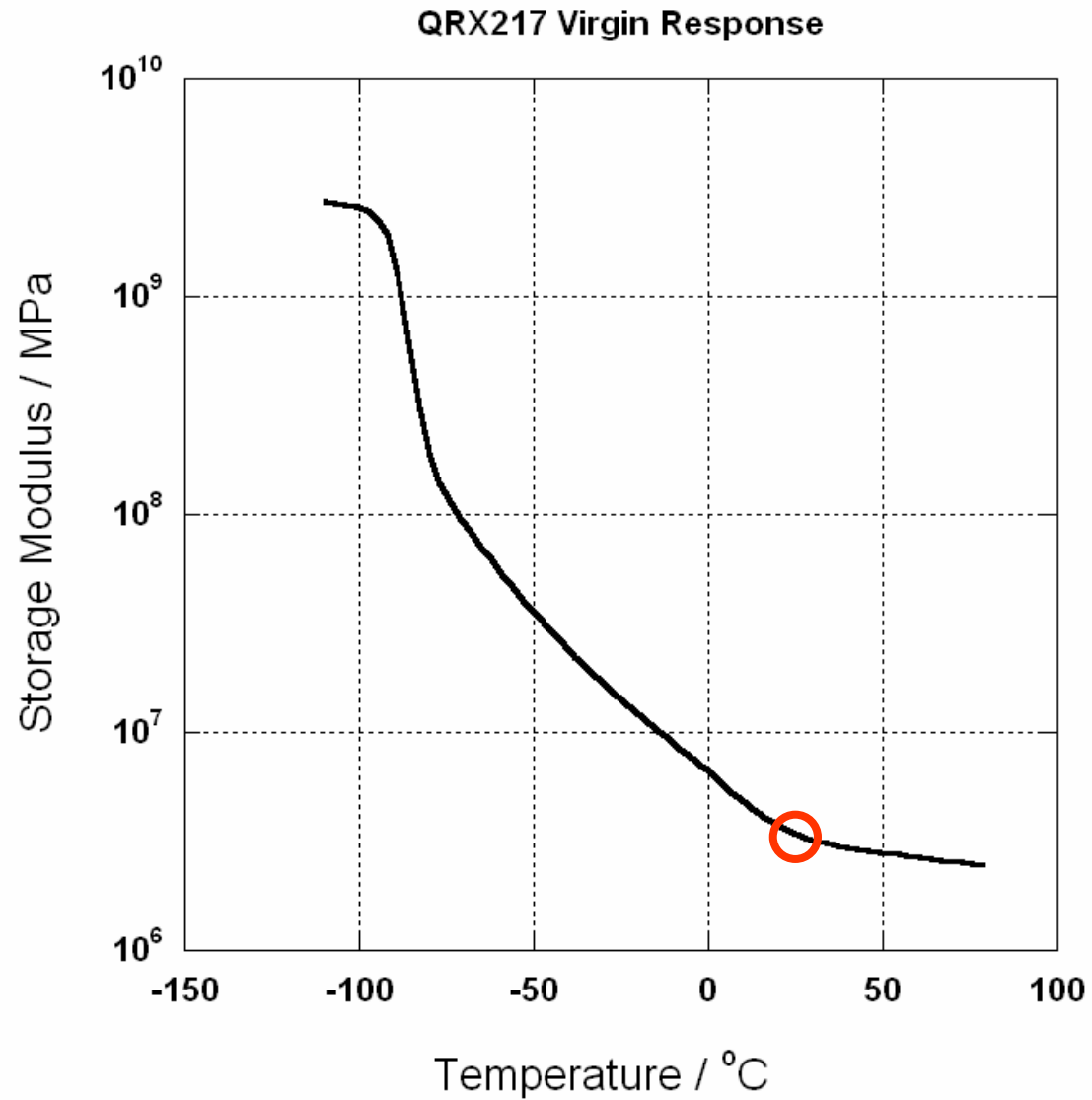
# Evaluating damaged samples



# Degradation of thermal conductivity

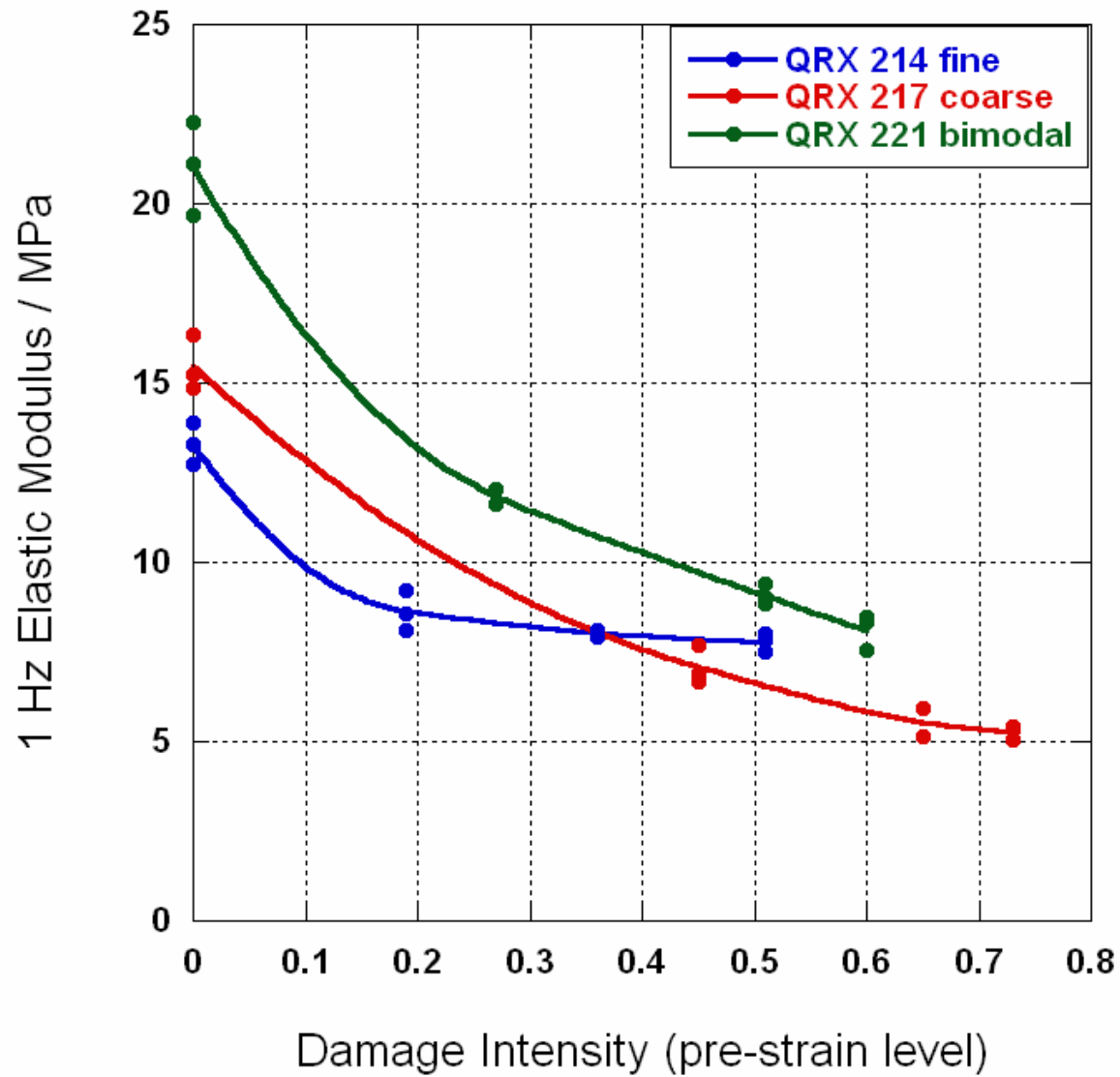


# Virgin DMA Spectra

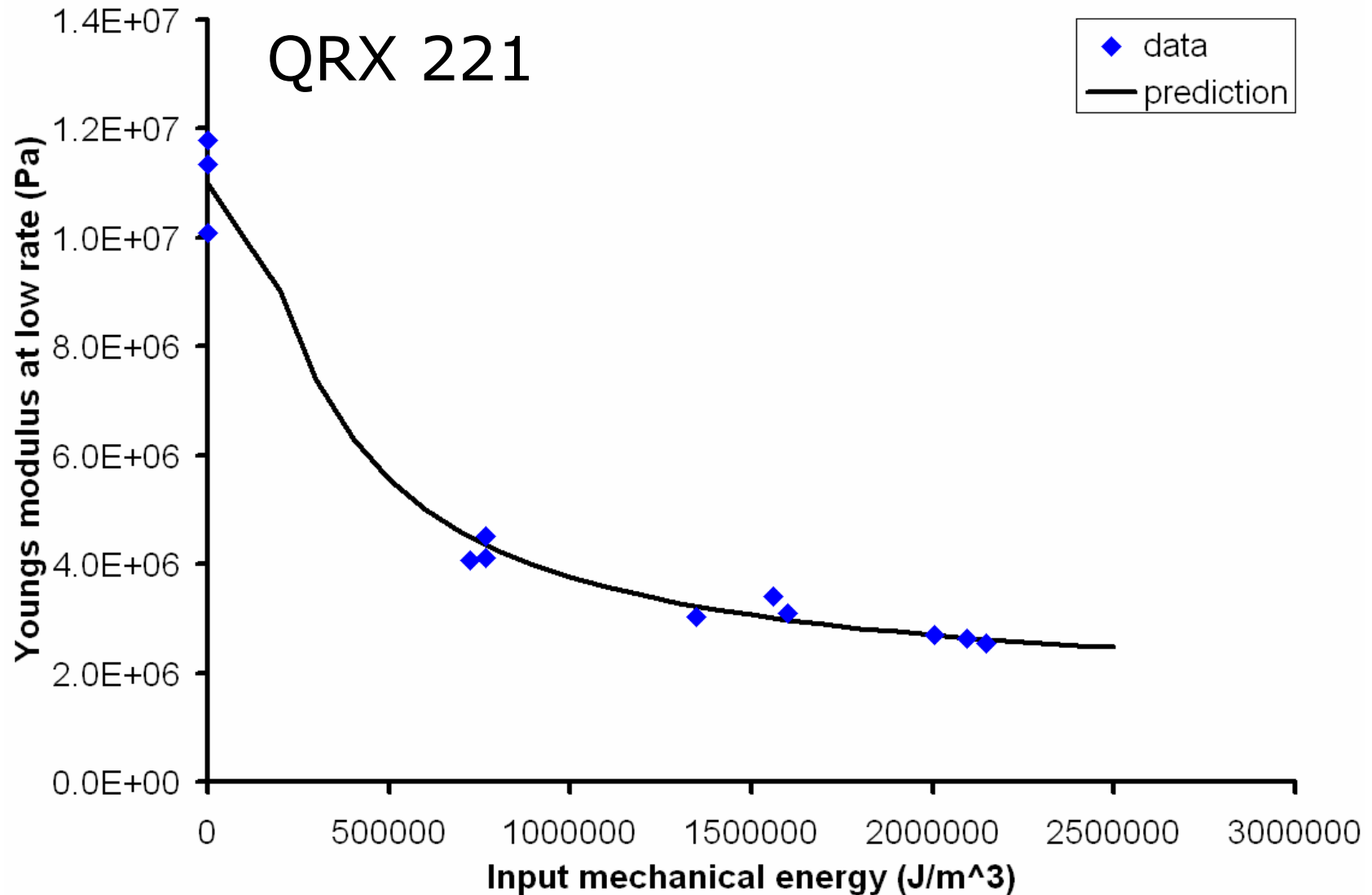




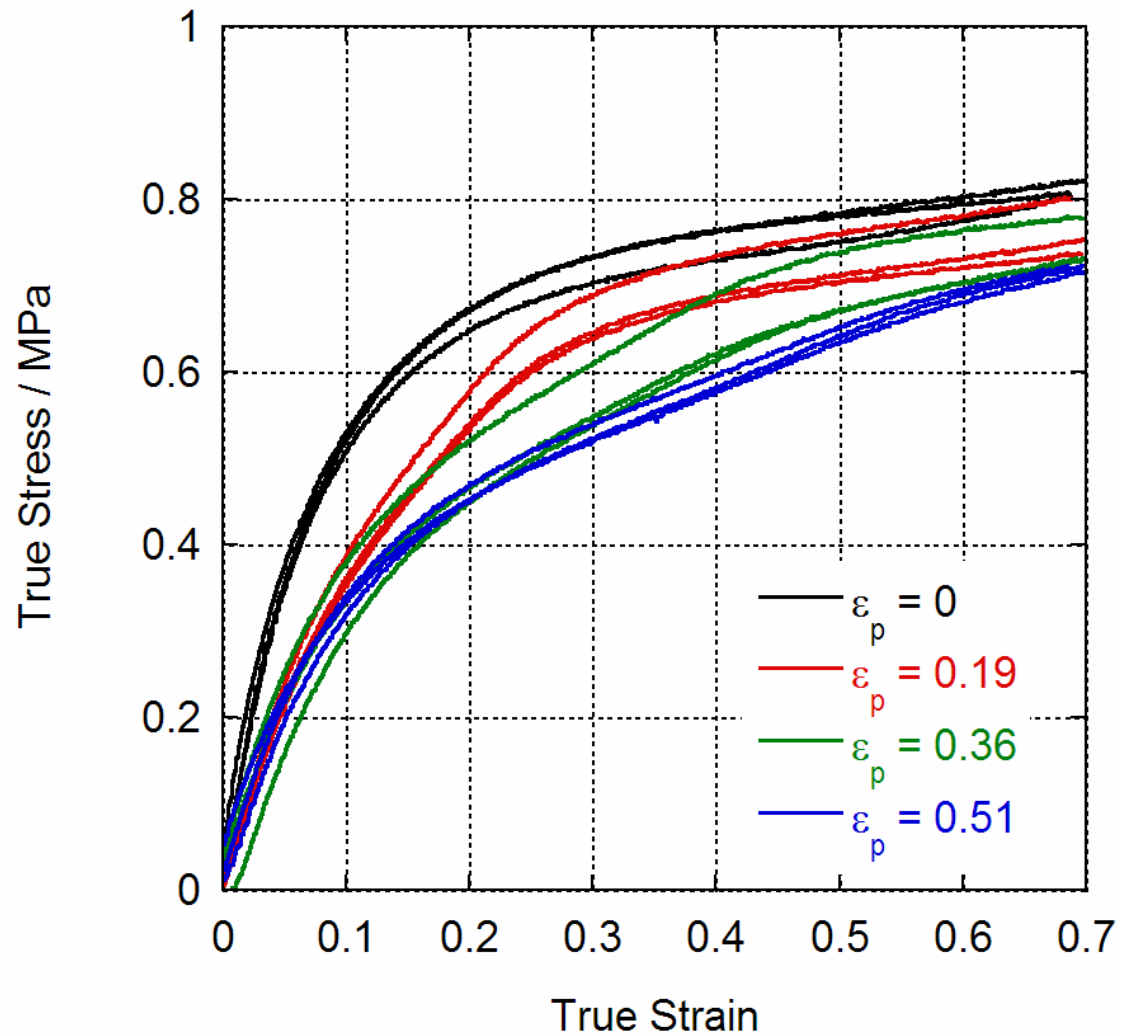
# Degradation of DMA Spectra



# Predicted degradation of modulus

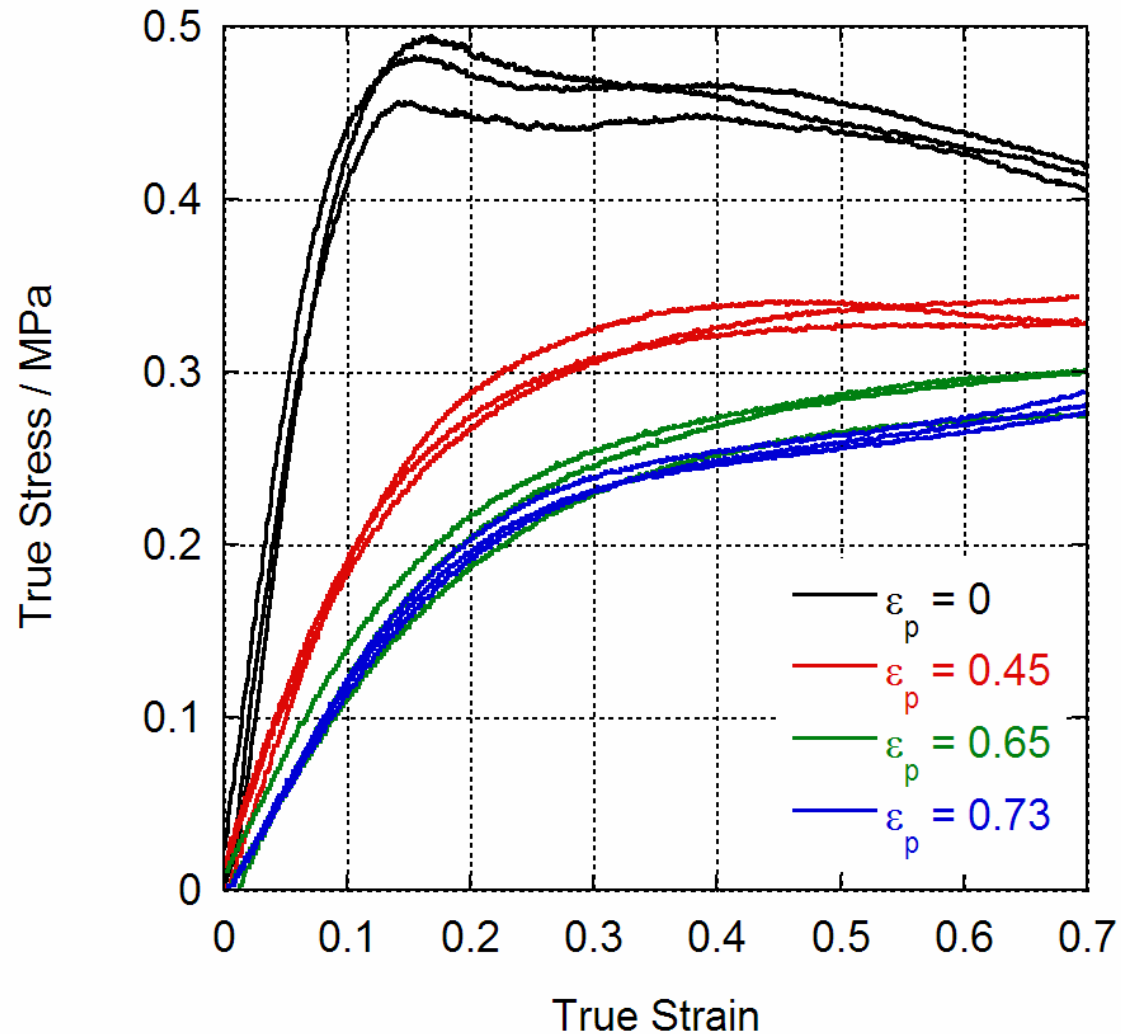


# Degradation of strength



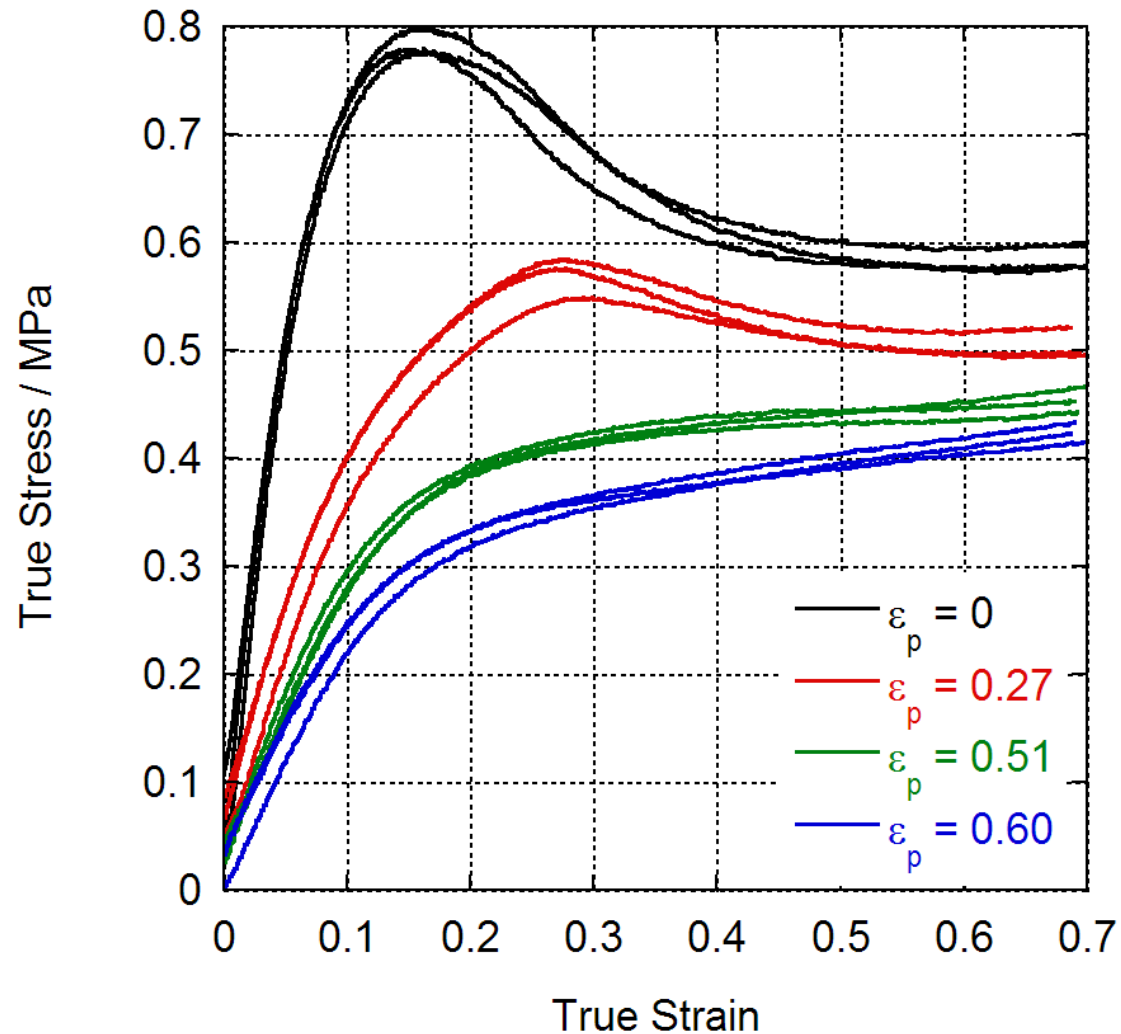
Low-rate response of QRX214 (monomodal fine)

# Degradation of strength



Low-rate response of QRX217 (monomodal coarse)

# Degradation of strength



Low-rate response of QRX221 (bimodal-fill)

# Summary

# Summary

Together with our sponsors, we at the Cavendish Laboratory are interested in understanding the full thermo-mechanical responses PBX and related materials, specifically by conducting insightful experiments.

The philosophy behind research is to get at the physical causes behind the experimental observations at the most fundamental level possible. Our colleagues in industry are approaching this from the direction of modeling.

Clearly understanding damage is very important, and here at the Cavendish, with the support of our sponsors, we feel we are making significant progress towards our goals.

A key attribute of the approach is the transferability of the techniques and understanding to be able to rapidly characterise new materials of all types.

# Acknowledgements

- ISP for opportunity to present
- AWE for funding, samples and scientific input  
(*Steve Wortley & Rebecca Govier*)
- QinetiQ for funding, samples and scientific input<sup>†</sup>  
(*Ian Cullis, Peter Gould and Phillip Church*)
- EPSRC for funding and equipment
- PCS members past and present

<sup>†</sup> This research was carried out as part of the Defence Technology  
Innovation Centre Weapons Research Programme: UK-E: Hazard



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